STUDY ON AXIAL COMPRESSION BEARING CAPACITY OF REINFORCED CONCRETE FILLED STEEL TUBE MEMBERS

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ABSTRACT: The bearing capacity equation of reinforced concrete filled steel tube (RCFST) members under axial loads is derived by using the combined unified and limit equilibrium theories. The concrete strength increase due to the constraint effect of the steel tube is taken into account through the use of unified theory; whereas the concrete strength increase due to the constraint effect of the stirrups is considered through the use of the limit equilibrium theory. Three-dimensional nonlinear finite element analysis and experimental tests were carried out and the corresponding results are reported in this paper. The comparisons of the numerical, experimental and theoretical results show that there are in good agreement between these three different methods. However, the present theoretical analysis model is not only simple and convenient to use but also consistent with existing Chinese design codes for CFST columns.

Keywords: Reinforced concrete filled steel tube, Axial compression bearing capacity, Unified theory, Limit equilibrium theory, Finite element

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1. INTRODUCTION

Because of many advantages, concrete filled steel tubes (CFST) are very popular in high rise buildings, bridges and offshore structures. Extensive studies have been conducted on the static and dynamic analyses, and the fire performance of CFST members [1-10]. For example, Han et al. [1], Yu et al. [2], Dundu et al. [3], Dai et al. [4] studied the compressive strength of CFST members. Han et al. [1], Yu et al. [5], Prabhu et al. [6] investigated the axial compression performance of CFST members encased by various different materials, such as concrete, FRP and CFRP. Wang et al. [7] studied the behavior of fire-exposed CFST columns. More recently, Ma et al. [8] studied their seismic behavior of CFST columns. Based on these studies, Chinese Codes [11] for design of concrete filled steel tubular members has been developed in 2014.

A RCFST member is formed by filling a steel tube with reinforcement concrete. Because of the large size of the section the RCFST members may have smaller thickness of steel tube than CFST members, which can cause trouble in machining, construction and welding. Reinforced concrete filled steel tubes (RCFST) have been used in multi-story buildings, particularly, high-level buildings. Figure 1 shows a typical section of a steel tube column and the corresponding column layout of Shenzhen Jingji financial center, which is ranked as the tenth highest building in the world.

Some studies have been conducted on the static performance of RCFST columns [12-20]. Lie [14] gave the resistance of circular steel columns filled with bar-reinforced concrete. Chang et al. [15] and Zhu et al. [16] conducted experimental studies on the performance of steel-reinforced concrete-filled-steel tubular members. Wang et al. [18] studied on experimental performance twin-column RCFT pier. Endo et al. [19] and Xiamuxi et al. [20] obtained the evaluation for axial

compressive strength of RCFST columns and the results were validated using experimental data. But most studies on the mechanical properties at room temperature didn't consider the constraints of the stirrup on core concrete. And they just simply considered the superposition of steel tube, concrete and longitudinal reinforcement on the basis of a coefficient, not considering the synergy of steel tube and concrete.

Notations									
K	Lateral constant determined by tests, $K = 4$ usually	A_{cor}	Area of concrete confined by stirrups, $A_{cor} = \pi d_s^2 / 4$						
f_{ck}'	Axial compressive strength of concrete confined by concrete stirrup	f, f_c	Design strength of steel and concrete, respectively						
f_r	Lateral pressure on concrete surrounded by stirrups	$ heta^*$	Equivalent confining factor of multilayer stirrups						
A_{ss1}	Area of single-layer stirrup	α	Steel ratio						
f_{yv}	Tensile strength of stirrup	Ψ	Hollow ratio, $\psi = A_h / (A_c + A_h)$						
d_s	Ddiameter of concrete column surrounded by stirrups	f_{y}, f_{ck}	Characteristic strength of steel and concrete, respectively						
S	Spacing of stirrups	B, C							
A_{sso}	Equivalent reinforcement area of stirrup,	$ heta_{\!\scriptscriptstyle h}$	Standard value of confining factor,						
	$A_{sso} = \frac{\pi d_s A_{ss1}}{s}$		$\theta_h = \alpha_0 f_y / (1.1 f_{ck})$						
A_{c}, A_{h}	Area of concrete and hollow part in HCFST, respectively	$ heta$, $ heta_{ ext{l}}$	Confining factor of steel tube in CFST and RCFST respectively, and						
A_{c}, A_{s}	Area of concrete and steel tube		$\theta = \frac{A_S f_y}{A_c f_{ck}}, \theta_1 = \frac{A_S f_y}{A_c f_{ck}^*}$						
$ ho_{\scriptscriptstyle ec{v}}$	Stirrup ratio								
$f_{sc,,}f_{sc}$	Combined strength of CFST and RCFST, respectively	A_{sc}	Total area of RCFST, Asc=As+Ac						
A_{b}	Total area of reinforcement in RCFST	f_b	Yield strength of reinforcement in RCFST						

In this paper the behavior of RCFST members under axial compression bearing capacity is studied through the theoretical analysis, finite element simulation and experimental tests. A theoretical analysis model is developed by using the combined unified and limit equilibrium theories. The present theoretical analysis model is not only simple and convenient to use but also consistent with existing Chinese design codes [11] for CFST columns.

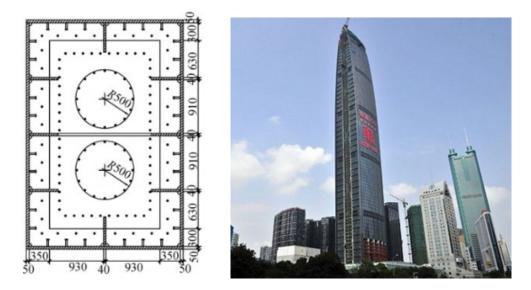
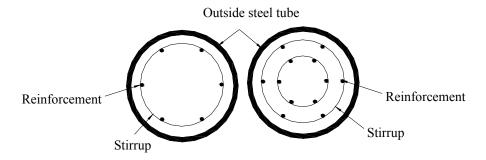


Figure 1. Typical Section of Steel Tube Column and Building Elevation of King Key Financial Center

2. THEORETICAL DERIVATION OF RCFST MEMBERS

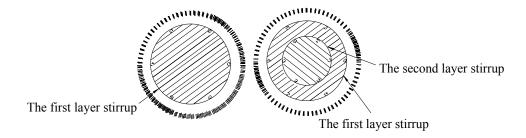
In general, the concrete in RCFST is restrained by both the outside steel tube and inside stirrups as shown in Figure 2. The constraints will enhance the concrete compressive strength, which will be discussed separately in the following analyses.



a) Single-layer reinforcement section b) Multilayer reinforcement section Figure 2. Cross Section Diagram of RCFST

2.1 The Equivalent Strength of Core Concrete from Stirrups

According to the configuration of the reinforcement, the core concrete of a RCFST member can be treated as a single layer material or a multilayer material, as shown in Figure 3. Both cases will be discussed in this paper. The equivalent strengths of the core concrete in both cases are to be developed.



a) Single-layer reinforcement section
 b) Multilayer reinforcement section
 Figure 3. Core Concrete Confined by Stirrups diagram of RCFST

2.1.1 The compressive strength of concrete confined by stirrups

(1) Axial compressive strength of concrete confined by single-layer stirrups

According to limit equilibrium theory from the theory of reinforcement concrete, if the spacing of spiral stirrups or welded stirrups is not larger than 80 mm and $d_s/5$ (where d_s is the diameter of the concrete column surrounded by stirrups), the strength improvement of core concrete due to the effect of stirrups should be considered (Slater et al. [21]), as shown in Figure 4.

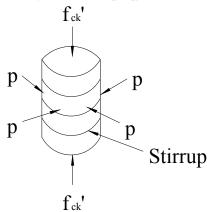


Figure 4. Concrete under Three-way Pressure

In this case, the longitudinal compressive strength of concrete confined by stirrups can be determined as follows:

$$f_{ck}' = f_{ck} + Kf_r \tag{1}$$

$$f_r = \frac{2A_{ss1}f_{yv}}{d_s s} \tag{2}$$

According to Eqs. 1, 2 and in general the lateral constraint coefficient is taken as K=4, it yields

$$f'_{ck} = f_{ck} \left(1 + \frac{2A_{ss0}}{A_{cor}} \cdot \frac{f_{yv}}{f_{ck}} \right) \tag{3}$$

Assuming ρ_{ν} is the stirrup reinforcement ratio, the confining factor of steel tube θ can be defined as follows

$$\theta = \rho_{v} \cdot \frac{f_{yv}}{f_{ck}} \tag{4}$$

So the axial compressive strength of the confined single-layer concrete stirrup can be expressed as:

$$f_{ck}' = f_{ck} \left(1 + 2\theta \right) \tag{5}$$

(2) Axial compressive strength of concrete confined by multilayer stirrups

Concrete in a RCFST column of multilayer stirrups can be divided into i+1 parts, as the shadow part shown in Figure 3 (b). As far as the whole member is concerned, the effects of individual layer stirrups on the concrete can be calculated using a superposition method. Hence, the ferrule effect increases gradually from outside to inside.

Assuming that A_{ci} is the area divided by the *i*th and (i+1)-th layer stirrups, θ_i is the ferrule coefficient of the *i*th layer stirrups, A_{ssoi} is the equivalent reinforcement area of the *i*th layer stirrups, ρ_v is the stirrup ratio, and f_{cki} is the concrete strength restrained by the *i*th layer stirrup, Eq. 4 can be expressed as follows

$$\theta_i = \rho_v \cdot \frac{f_{yv}}{f_{ck}} = \frac{A_{ssoi}}{A_{ci}} \cdot \frac{f_{yv}}{f_{ck}} \tag{6}$$

when
$$i = 1$$
, $f_{cki} = f_{ck} (1 + 2\theta_1)$ (7)

when
$$i > 1$$
, $f_{cki} = f_{ck} (1 + 2\sum_{k=1}^{i} \theta_k)$ (8)

According to the above formulas, the compressive strength of concrete confined by the multilayer stirrups is equal to the ordinary concrete strength multiplied a stirrup enhancement coefficient.

2.1.2 Equivalent strength of core concrete within the outside steel tube

The total bearing capacity of concrete within the steel tube including plain concrete with no stirrups and the concrete confined by stirrups can be given by Eq. 9, including the shadow and blank parts shown in Figure 3.

$$N_c = A_c f_{ck} + \sum_{i=1}^n A_{ci} \left(f_{cki} - f_{cki-1} \right) = A_c f_{ck} + 2 \sum_{i=1}^n A_{ci} f_{ck} \theta_i$$
(9)

Substituting Eq. (6) into (9), it yields

$$N_{c} = A_{c} f_{ck} + 2 \sum_{i=1}^{n} A_{ci} f_{ck} \frac{A_{ssoi}}{A_{ci}} \cdot \frac{f_{yv}}{f_{ck}} = A_{c} f_{ck} + 2 f_{yv} \sum_{i=1}^{n} A_{ssoi} = A_{c} f_{ck} \left(1 + 2\theta^{*} \right)$$
(10)

Since

$$\theta^* = \frac{f_{yv} \sum_{i=1}^n A_{ssoi}}{A_c f_{ck}} \tag{11}$$

Eq. 10 is simplified as follows

$$f_{ck}^* = \frac{N_c}{A} = f_{ck} \left(1 + 2\theta^* \right) \tag{12}$$

2.2 Axial Compression Bearing Capacity of RCFST by steel tube

2.2.1 Combined strength by steel tube

According to the CFST "unified theory" [13], the compressive strength of the CFST column can be expressed as follows:

$$f_{sc} = (1.212 + B\xi + C\xi^2) f_{ck}$$
(13)

The strength of concrete in Eq. 12 replacing 13, we have the formula of the combined strength of RCFST columns:

$$f_{sc}' = (1.212 + B_1 \xi_1 + C_1 \xi_1^2) f_{ck}^* = (1.212 + B_1 \xi_1 + C_1 \xi_1^2) f_{ck} (1 + 2\theta^*)$$
(14)

where,
$$\xi_1 = \frac{A_s f_y}{A_c f_{ck}^*}$$
, $B = B_1 = 0.1759 \frac{f_y}{235} + 0.974$, $C = -0.1038 \frac{f_{ck}}{20.1} + 0.0309$ and $C_1 = -0.1038 \frac{f_{ck}}{20.1} + 0.0309$.

2.2.2 Axial compression bearing capacity

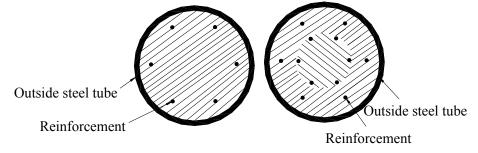


Figure 5. Cross Section Diagram of RCFST without Stirrup

According to superposition principle, the axial compression bearing capacity of RCFST members is obtained by the sum of the axial compression bearing capacity of longitudinal bar and CFST members confined by stirrups, as shown in Figure 5.

$$N_{scb} = A_{sc} f'_{sc} + A_b f_b = A_{sc} \left(1.212 + B_1 \xi_1 + C_1 \xi_1^2 \right) f_{ck} \left(1 + 2\theta^* \right) + A_b f_b \tag{15}$$

The above description demonstrates that the axial compression bearing capacity of RCFST members is related to the ferrule coefficient of stirrups and steel tube, reinforcement ratio and strength of longitudinal reinforcement. If the ferrule coefficient or the reinforcement ratio becomes higher, the overall load-bearing capacity becomes stronger.

2.2.3 Compared with the formula of national code when it is CFST

When the reinforcement ratio is zero, the RCFST reduces to the CFST. Because $A_b = 0$ and $\theta^* = 0$, Eq. 15 is simplified into Eq. 16.

$$N_{scb} = A_{sc} f'_{sc} + A_{b} f_{b}$$

$$= A_{sc} (1.212 + B_{1} \xi_{1} + C_{1} \xi_{1}^{2}) f_{ck}$$

$$= A_{sc} (1.212 + B \xi + C \xi^{2}) f_{ck}$$

$$= A_{sc} f_{sc}$$
(16)

By comparing Eqs. 13 and 16, it can be seen that the formula of RCFST is in a good agreement with the formula recommended in Chinese design code for CFST members. Furthermore Eq. 15 can be regarded as an extension of the Chinese national design code for RCFST members.

3. FINITE ELEMENT SIMULATION OF RCFST MEMBERS

3.1 The material constitutive relation

Core concrete of RCFST is simulated by using the plastic-damage constitutive model (Ludovic et al. [22]). The uniaxial compressive stress-strain model of concrete is utilized as suggested by Hognestad (Jeffrey et al. [23]), which is simplified as the elastic-perfectly plastic model, as shown in Figure 6. Tensile in elastic part is similar with compressive parts, and the ultimate tensile strength is taken as one-tenth of the compressive strength. The steel model uses the bilinear model. Poisson's ratio is taken as 0.25 for concrete and 0.3 for steel.

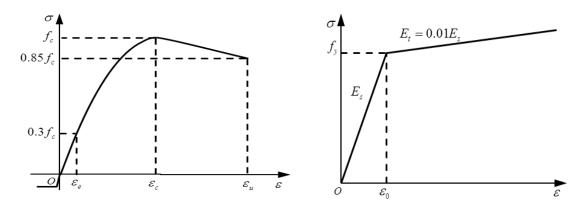


Figure 6. The Constitutive Relation of Concrete and Steel

3.2 The Finite Element Model

The three-dimensional solid element (C3D8R) is used to simulate the core concrete and steel tube of CFST members (Lu and Zhao [24]). The truss element (T3D2) is adopted to simulate the

unidirectional reinforced bars. For the convenience of applying boundary conditions, two rigid circular plates are used in the finite element analysis (FEA) model to simulate the upper and lower cover plates of the CFST member. All boundary conditions and loads are directly loaded on the rigid plates. Reinforced skeleton frame and concrete are contacted by using the Embedded region defined in ABAQUS. Element meshes of core concrete and reinforcement are shown in Figure 7.

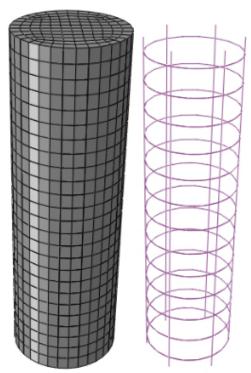


Figure 7. Model Meshes of Core Concrete and Reinforcement

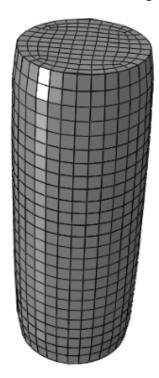


Figure 8. Deformation Model

Fixed displacement constraints are imposed to the bottom rigid plate. On the top rigid plate all other degrees of freedom except for the axial displacement are fixed. The axial loading is added on the center of the top plate. The problem is solved by using the displacement loading method.

3.3 Finite Element Results

Before the parametric analysis of the finite element analysis, finite element model is verified in this section. From the comparison between finite element simulation and its theoretical value under different parameters, it is found finite element value is slightly higher than the theoretical value, but the error is very small. Figure 8 plots a typical deformed shape of the RCFST column.

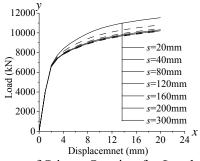


Figure 9. The Influence of Stirrup Spacing for Load-displacement Curve

Figure 9 shows the influence of the number of stirrups on the ultimate bearing capacity of the RCFST column (Wang [25]). It can be seen from the figure that the ultimate load increases with the decrease of the spacing of the stirrups. Table 1 gives a comparison of the finite element results with the theoretical values. Through the parameter analysis, it is found that the influence of the steel tube ferrule coefficient and slenderness ratio on the load-displacement curve of RCFST members are similar to CFST members.

According to the results of finite element simulation, reinforcement ratio, the strength of longitudinal reinforcement and the stirrup spacing are the key parameters, which should be considered in the experimental tests.

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Steel ratio α	Steel pipe intensity f_y (MPa)	Concrete strength f_{ck} (MPa)	Reinforcement ratio ρ_b	Longitudinal reinforceme nt intensity $f_b(\text{MPa})$	Stirrup spacing s (mm)	Theoretical value N_c (kN)	Simulation value N_0 (kN)	N_0/N_c
0.080	235	33.5	0.027	335	80	9455	9757	1.032
0.080	235	40.2	0.027	335	80	10489	10732	1.023
0.080	235	46.9	0.027	335	80	11526	11657	1.011
0.080	345	20.1	0.027	335	80	8825	9039	1.024
0.080	390	20.1	0.027	335	80	9443	9581	1.015
0.080	420	20.1	0.027	335	80	9865	9942	1.008
0.019	235	20.1	0.027	335	80	5631	5598	0.994
0.039	235	20.1	0.027	335	80	6248	6367	1.019
0.059	235	20.1	0.027	335	80	6837	7066	1.034
				Mean value				1.028

4. AXIAL COMPRESSION TEST RESEARCH

4.1 General Situation of Test

4.1.1 Material

Tensile tests of reinforcement and steel tube were carried out by using hydraulic universal material testing machine. The sample size was determined according to the tensile test of metallic materials. The length of reinforcement specimens is 500 mm. Figure 10 shows some of the specimens tested for the steel tube and reinforcement. The specimens tested for concrete is shown in Figure 11 (Wang [25]), which is the standard cubic specimen of 150*150*150 mm.



a) Steel tube specimens

b) Reinforcement material specimens

Figure 10. Steel Specimens



Figure 11. Concrete Standard Cube Specimens

The yield and ultimate strengths for the steel were obtained in the steel tensile tests, which show that both the steel tube and reinforcement have very good ductility. The concrete cubic compressive strength f_{ck} is used to calculate the compressive strength of the prism by using $f_{ck} = k_2 f_{cu,k}^{150}$ (where k_2 is the conversion factor, for ordinary strength concrete, $k_2 = 0.67$).

4.1.2 Specimens

The axial compressive tests included CFST specimens and RCFST specimens, and all steel tubes were of the same size. RCFST specimens were divided into three groups according to the strength of internal longitudinal reinforcement, and there were three kinds of longitudinal reinforcement ratios and two stirrup spacings in each group specimens. The section size of the cover plates was $500 \text{mm} \times 500 \text{mm}$, with an identical thickness of 16 mm. All parameters of specimens are listed in Table 2.

The experiment was carried out in architecture lab of South China University of Technology. The specimens were made by the procedure: (1) fabrication of steel reinforcement cage, (2) welding reinforcement to the bottom plate, (3) welding steel tube to the bottom plate, (4) pouring concrete into the steel tube. During the casting of concrete, a 50 mm plug-in vibrator was used to vibrate the concrete. After the concrete is casted, the specimen was cured for 12 hours in an environment with fixed temperature and humidity conditions. After the concrete was cured, the top steel plate was welded to the specimen (Jamaluddin et al. [26]).

Table 2. Parameters of the Specimens under Axial Compression

Sample number	$D(\mathrm{mm})$	t (mm)	L (mm)	f_y (MPa)	f_{cu} (MPa)	f_b (MPa)	f_{yv} (MPa)	$ ho_{\!\scriptscriptstyle b}$	s (mm)
A-1	426	8	1300	297	28.24	-	-	0	-
A1-6-1	426	8	1300	297	28.24	414	314	1.73%	100
A1-10-1	426	8	1300	297	28.24	414	314	2.88%	100
A1-10-2	426	8	1300	297	28.24	414	314	2.88%	50
A1-12-1	426	8	1300	297	28.24	414	314	3.45%	100
A2-6-1	426	8	1300	297	28.24	485	314	1.73%	100
A2-10-1	426	8	1300	297	28.24	485	314	2.88%	100
A2-10-2	426	8	1300	297	28.24	485	314	2.88%	50
A2-12-1	426	8	1300	297	28.24	485	314	3.45%	100
A3-6-1	426	8	1300	297	28.24	532	314	1.73%	100
A3-10-1	426	8	1300	297	28.24	532	314	2.88%	100
A3-10-2	426	8	1300	297	28.24	532	314	2.88%	50
A3-12-1	426	8	1300	297	28.24	532	314	3.45%	100

Note: In the table, D is the cross-section diameter of the specimen, t is thickness the steel tube L is the length of members, f_y is the yield strength of steel, f_{cu} is the cube crushing strength of concrete, f_b is yield strength of the longitudinal reinforcement, f_{yy} is the yield strength of stirrup, ρ_b is the ratio of longitudinal reinforcement, f_y is the stirrup spacing.

4.1.3 Test procedure

(1) The test instrument and equipment Axial compression tests were performed in the 1500T hydraulic pressure testing machine, as shown in Figure 12. Collecting device of strains and displacements was DH3816 static strain gauge.





Figure 12. 1500T Hydraulic Pressure Testing Machine

(2) Loading and data acquisition In the axial compression test, the parameters needed to determine were the longitudinal stress-strain relationship of reinforcement, the stress-strain relationship of the steel tube in both the longitudinal and hoop directions. In order to obtain the required parameters, four groups of strain gauges were placed on the middle of the external surface of the steel tube, which were purposed to measure the longitudinal and hoop strains (see Figure 13).

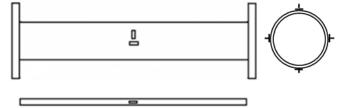


Figure 13. Strain Gauge Arrangement of Steel Tube and Reinforcement

In addition, four internal longitudinal strain gauges were used to measure the axial tension and compression strain of longitudinal reinforcement (Nie et al. [27]). To determine the axial and lateral displacements of the specimens, two axial displacement meters and two lateral displacement meters were placed in the middle of the column (Hou et al. [28]).

4.2 Experimental Results

In the axial compression test process, short columns generally do not fall, so when the axial displacement component reaches a certain extent or when the axial deformation is large, the test is stopped or unloaded.



Figure 14. Slip Line and Failure State

The experimental phenomenon (Figure 14) shows that the damage form of RCFST specimens is neither bending failure nor shear failure, but the local buckling. The examination of the internal concrete shows that there is no evidence of debonding from the steel tube although concrete crushing in some places.

A detailed comparison of the theoretical, finite element analysis and experimental results of the short column is given in Table 3. It can be seen from Figure 15 that the ductility of the RCFST members is better than that of CFST members. For such good ductile structural members it is general to take the compressive load at the strain value of 0.0035 as the bearing load of the member (Degtyarev [29]).

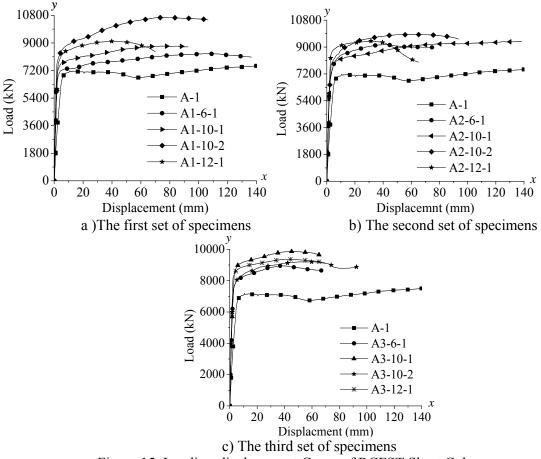


Figure 15. Loading-displacement Curve of RCFST Short Columns

Specimen number	Theoretical value $N_c(kN)$	Finite element value N_0 (kN)	Trial value $N_e(kN)$	N_c/N_0	N_c/N_e
A1-1	6760	6791	6826	0.996	0.990
A1-6-1	8042	8045	8302	1.000	0.969
A1-10-1	8637	8676	8797	0.995	0.982
A1-10-2	9056	9077	9946	0.998	0.911
A1-12-1	8934	8999	9215	0.993	0.970
A2-6-1	8204	8205	8896	1.000	0.922
A2-10-1	8907	8943	9375	0.996	0.950
A2-10-2	9326	9344	9847	0.998	0.947
A2-12-1	9258	9320	9400	0.993	0.985
A3-6-1	8311	8311	8748	1.000	0.950
A3-10-1	9085	9118	9594	0.996	0.947
A3-10-2	9505	9521	9388	0.998	1.012
A3-12-1	9473	9532	9488	0.994	0.998
	Mean		0.997	0.964	

Table 3. Axial Compression Bearing Capacity of Short Columns

5. CONCLUSIONS

This paper has presented the theoretical, numerical and experimental investigations on the ultimate bearing load capacity of RCFST columns. The theoretical study is performed by using the combined unified and limit equilibrium theories. The numerical study is done by using the finite element method. The theoretical and FEA results are validated by the experimental data. From the results obtained the following conclusions can be drawn:

- 1) Addition of longitudinal reinforcement in RCFST short columns can significantly increase the bearing capacity of the columns, in which both longitudinal reinforcement and stirrups play important role in this strength increase.
- 2) Short columns are neither in bending failure nor in shear failure, but in the local buckling failure of the steel tube.
- 3) The proposed theoretical formula for calculating the compressive strength of RCFST columns is consistent with existing design code for CFST columns. That is, it reduces to the design formula of CFST when the reinforcement ratio is 0.

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