

# NUMERICAL ANALYSIS OF PLAIN AND STEEL FIBER REINFORCED CONCRETE FILLED STEEL TUBULAR SLENDER COLUMN

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**ABSTRACT:** Concrete filled steel tube columns (CFST) have many potentials which include; high seismic resistance, high load bearing capacity, and fire resistance without external protection. Some major projects worldwide has adopted the use of this type of column member extensively, for columns in both the gravity systems and the seismic resisting systems. Experimental tests performed on concrete filled steel tube columns at ambient temperature indicates that, the use of steel fibre reinforced concrete infill affects the crack width propagation of the concrete. This paper presents an advanced 3D numerical model which predicts the behaviour of a CFST column filled with steel fibre reinforced concrete, taking into account the increased tensile strength of the concrete which affects the column ductility. For columns subjected to compression loading only, it is recommended to use a high strength concrete, and also increase the thickness of the steel tube rather than using a steel tube with a higher yield strength. For slender square columns loaded under large eccentricity, it is recommended to use an  $e/D$  (eccentricity/depth) ratio value less than 0.5 for design purposes, to avoid the premature fracture of the loaded end of the column having smaller steel tube thickness.

**Keywords:** Concrete filled tubular columns, steel fibre reinforced concrete, finite element analysis, composite column, square hollow steel section

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## 1. INTRODUCTION

Concrete filled steel tube (CFST) columns are an increasingly popular form of construction. The advantages of CFST include a high compression strength, good ductility, reduction in size of the column, ease of construction and potential fire resistance ratings (Zhao et al. [1]). The 1995 Kobe earthquake in Japan influenced the emphasis on CFST construction whereby, emphasis was placed on ductility, energy absorption and performance in seismic zones (Kitada [2]).

Steel tube local buckling is one of the critical issues to consider when designing a steel tube column. Researchers have indicated that addition of a concrete infill to the steel tube will reduce the effects of local buckling (Brauns [3], Ellobody, Young and Lam [4]). Steel fiber reinforced concrete infill is a popular type of concrete infill due to the advantages of increasing the tensile strength of the concrete and controlling the crack width of the concrete core (Ellobody [5], Zhao et al. [6]). Comprehensive experimental and numerical experiments conducted by (Zeghiche and Chaoui [7]) together with (Johansson and Gylltoft [8]), showed that it is possible to achieve ductility in the column by also using concrete strength higher than 50MPa.

Ellobody [5], showed that addition of fiber to plain concrete increases its flexural and tensile strength, which results in superior post-elastic material properties. The various parameters that affect the behaviour of steel fiber reinforced concretes which includes its matrix strength, fiber type, fiber Young's modulus, fiber dosage and fiber tensile strength. Figure 1 shows a comparison between the stress - strain curve of plain and steel fiber reinforced concrete.

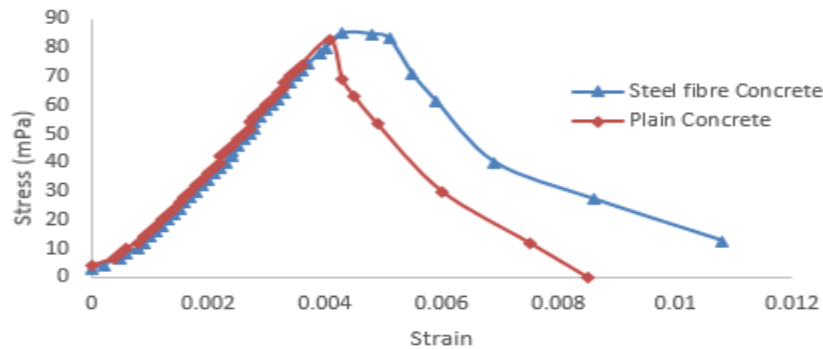


Figure 1. Comparison of Stress–strain Curves of Plain and SFR Concrete

Eltobgy [9], observed that the use of steel fibre reinforced concrete improved the structural stability of a CFST columns and the slenderness ratio is also an important factor that govern its behaviour.

Gopal and Manoharan [10], carried out tests on 12 slender circular steel tubular columns filled with both plain and steel fiber reinforced concrete. The specimens were tested under eccentric axial loading to investigate the effects of fiber reinforced concrete on the ultimate strength and behaviour of the composite columns. It was reported that the use of fiber reinforced concrete as infill for tubular steel gives the column additional strength and ductility.

Tokgoz and Dundar [11], conducted experimental tests on 16 concrete filled steel tubular columns, each tubular column was filled with either plain or steel fibre reinforced concrete. The columns were loaded axially with different levels of eccentricity having an  $e/D$  ratio between 0.5-0.67 where  $e$  is the eccentricity and  $D$  is the depth or height of the column. It was reported that the inclusion of steel fiber to the concrete improved the ductility and deformation of the column. The steel fibres, however, had little effect on the ultimate strength capacity of the column.

The main objective of the study reported herein is to investigate numerically the behaviour of axially loaded steel fiber reinforced CFST column. The numerical model is validated by comparison with experimental data reported in the literature, and also the Eurocode 4 part 1-1 [12] design model. Sixteen composite columns were simulated from experimental tests carried out by Tokgoz and Dundar [11] from the literature and the main variables for the columns were the cross-section, slenderness, concrete compressive strength and the load eccentricity. The ultimate strength and load-deflection profile of the columns were analysed and compared to the experimental results. A parametric study was also carried out to investigate the influence of the steel yield strength, steel tube thickness and concrete compressive strength to the ultimate strength and ductility of the column.

## 2. FINITE ELEMENT MODELLING

### 2.1 General

To analyse the behaviour of plain and steel fiber reinforced CFST column, A three dimensional non-linear finite element CFST column was modelled using ABAQUS [13].

A total of 38 CFST columns were modelled; 16 of these columns were from the literature which was used to validate the numerical simulation. The remaining 22 were used for the parametric studies. All the columns were of length of 1250 mm which had similar length with the experimental study. The material properties and geometry of the columns are summarized in Table 1(a) and (b). The slenderness ( $\lambda$ ), concrete cylindrical compressive strength ( $f_c$ ), steel yield strength and ultimate tensile strength ( $f_y$  &  $f_u$ ) and steel ratio ( $\delta$ ) are also shown.

Table 1a. ABAQUS CFST Column Model for Validating Experimental Study

S/N	B x D x t mm	B/t	e/D	L/D	$e_x$ mm	$e_y$ mm	$\lambda$	$\delta$	$f_c$ MPa	$f_y$ MPa	$f_u$ MPa
1	60 x 60 x 5	12.00	0.50	20.83	30	30	0.76	0.71	51.48	290	360
2	60 x 60 x 5	12.00	0.50	20.83	30	30	0.77	0.70	54.13	290	360
3	60 x 60 x 5	12.00	0.67	20.83	40	40	0.77	0.69	56.24	290	360
4	60 x 60 x 5	12.00	0.67	20.83	40	40	0.77	0.69	58.67	290	360
5	70 x 70 x 5	14.00	0.50	17.86	35	35	0.66	0.67	51.48	290	360
6	70 x 70 x 5	14.00	0.50	17.86	35	35	0.66	0.66	54.13	290	360
7	70 x 70 x 5	14.00	0.64	17.86	45	45	0.67	0.65	56.24	290	360
8	70 x 70 x 5	14.00	0.64	17.86	45	45	0.67	0.64	58.67	290	360
9	80 x 80 x 4	20.00	0.50	15.63	40	40	0.59	0.57	51.48	290	360
10	80 x 80 x 4	20.00	0.50	15.63	40	40	0.60	0.56	54.13	290	360
11	80 x 80 x 4	20.00	0.63	15.63	50	50	0.60	0.55	56.24	290	360
12	80 x 80 x 4	20.00	0.63	15.63	50	50	0.61	0.54	58.67	290	360
13	100 x 100 x 4	25.00	0.50	12.50	50	50	0.48	0.51	51.48	290	360
14	100 x 100 x 4	25.00	0.50	12.50	50	50	0.49	0.49	54.13	290	360
15	100 x 100 x 4	25.00	0.60	12.50	60	60	0.49	0.48	56.24	290	360
16	100 x 100 x 4	25.00	0.60	12.50	60	60	0.50	0.47	58.67	290	360

Table 1b. ABAQUS CFST Column Model for Parametric Study

S/N	B x D x t mm	B/t	e/D	L/D	$e_x$ mm	$e_y$ mm	$\lambda$	$\delta$	$f_c$ MPa	$f_y$ MPa	$f_u$ MPa
1	100 x 100 x 4	25.00	0.00	12.50	0	0	0.48	0.51	50.10	290	360
2	100 x 100 x 4	25.00	0.00	12.50	0	0	0.49	0.50	52.17	290	360
3	100 x 100 x 4	25.00	0.25	12.50	25	25	0.48	0.51	50.10	290	360
4	100 x 100 x 4	25.00	0.25	12.50	25	25	0.49	0.50	52.17	290	360
5	100 x 100 x 4	25.00	0.00	12.50	0	0	0.51	0.56	50.10	350	430
6	100 x 100 x 4	25.00	0.00	12.50	0	0	0.51	0.55	52.17	350	430
7	100 x 100 x 4	25.00	0.25	12.50	25	25	0.51	0.56	50.10	350	430
8	100 x 100 x 4	25.00	0.25	12.50	25	25	0.51	0.55	52.17	350	430
9	100 x 100 x 4	25.00	0.50	12.50	50	50	0.51	0.55	51.48	350	430
10	100 x 100 x 4	25.00	0.50	12.50	50	50	0.51	0.54	54.13	350	430
11	100 x 100 x 6	16.67	0.00	12.50	0	0	0.46	0.63	50.10	290	360
12	100 x 100 x 6	16.67	0.00	12.50	0	0	0.47	0.62	52.17	290	360
13	100 x 100 x 6	16.67	0.25	12.50	25	25	0.46	0.63	50.10	290	360
14	100 x 100 x 6	16.67	0.25	12.50	25	25	0.47	0.62	52.17	290	360
15	100 x 100 x 6	16.67	0.50	12.50	50	50	0.47	0.62	51.48	290	360
16	100 x 100 x 6	16.67	0.50	12.50	50	50	0.47	0.61	54.13	290	360
17	100 x 100 x 6	16.67	0.00	12.50	0	0	0.49	0.67	50.10	350	430
18	100 x 100 x 6	16.67	0.00	12.50	0	0	0.50	0.66	52.17	350	430
19	100 x 100 x 6	16.67	0.25	12.50	25	25	0.49	0.67	50.10	350	430

20	100 x 100 x 6	16.67	0.25	12.50	25	25	0.50	0.66	52.17	350	430
21	100 x 100 x 6	16.67	0.50	12.50	50	50	0.49	0.66	51.48	350	430
22	100 x 100 x 6	16.67	0.50	12.50	50	50	0.50	0.65	54.13	350	430

The steel contribution ratio  $\delta$  and slenderness  $\lambda$  were calculated based on Eurocode 4 Part 1.1 [12] as follows.

$$\delta = \frac{A_a \times f_y}{N_{pl}} \quad (1)$$

Where  $A_a$  is the area of steel and  $N_{pl}$  is the squash load of the column.

$$\lambda = \sqrt{\frac{N_{pl}}{N_{cr}}} = \sqrt{\frac{A_c f_c + A_a f_y}{\frac{\pi^2 EI}{L^2}}} \quad (2)$$

Where  $A_c$  is the area of concrete and  $EI = E_s I_s + 0.6 E_{cm} I_c$ ;  $I_s$  and  $I_c$  are the second moment of inertia of the steel tube and concrete core respectively,  $E_s$  is the modulus of elasticity of steel and  $E_{cm}$  is the secant modulus of elasticity of concrete.

The CFST models were classified into six sets, Sb-t-e-f<sub>y</sub>-I-P, Sb-t-e-f<sub>y</sub>-III-P and Sb-t-e-f<sub>y</sub>-V-P were modelled without using steel fibres, while a 0.75% volume of steel fiber was added to model Sb-t-e-f<sub>y</sub>-II-SF, Sb-t-e-f<sub>y</sub>-IV-SF and Sb-t-e-f<sub>y</sub>-VI-SF. The following label were used; “Sb-t-e-f<sub>y</sub>-f<sub>c</sub>-p/sf” where “b” is the columns breadth, “t” is the steel tube thickness “e” is the eccentric distance of the applied axial load, “f<sub>y</sub>” is the steel yield strength, “f<sub>c</sub>” is the concrete cylindrical strength, “p/sf” indicates whether it is a plain or steel fibre reinforced concrete infill.

## 2.2 Finite Element Mesh and Geometry

The main parameters of the model are the column breadth (B), the depth (D), the steel tube thickness (t) and the loading eccentricity (e). The plain and steel fiber CFST columns were modelled using shell and solid elements. The steel tube consisted of four-nodded quadrilateral shell element (S4R), while eight-nodded solid elements (C3D8R) with reduced integration were used for the concrete core. The loading end plate was modelled as rigid (R3D4) to enable an even stress distribution of the eccentric axial load to the column.

## 2.3 Boundary Condition and Column Loading

The column was modelled with a pin-pin end condition. A reference point was created on the loading plate to indicate the position of the ex and ey eccentric distance of the applied load.

## 2.4 Material Modelling of Steel Tube

The stress–strain curves for the steel tubes were taken from values used in the experimental tests conducted by Tokgoz and Dundar [11]. A modulus of elasticity of 200GPa and Poisson’s ratio of 0.3 was employed. The yield stress and ultimate tensile strength values are also shown in Table 1(a) and (b) above.

## 2.5 Modelling of Confined Concrete

The concrete core was modelled using the concrete damaged plasticity (CDP) model available

in the standard and explicit material library (ABAQUS [13]). The concrete damaged plasticity model uses stress-strain relationships to correlate parameters for relative concrete damage for both tension and compression under uni-axial loading as shown in Figures 2(a) and 2(b).

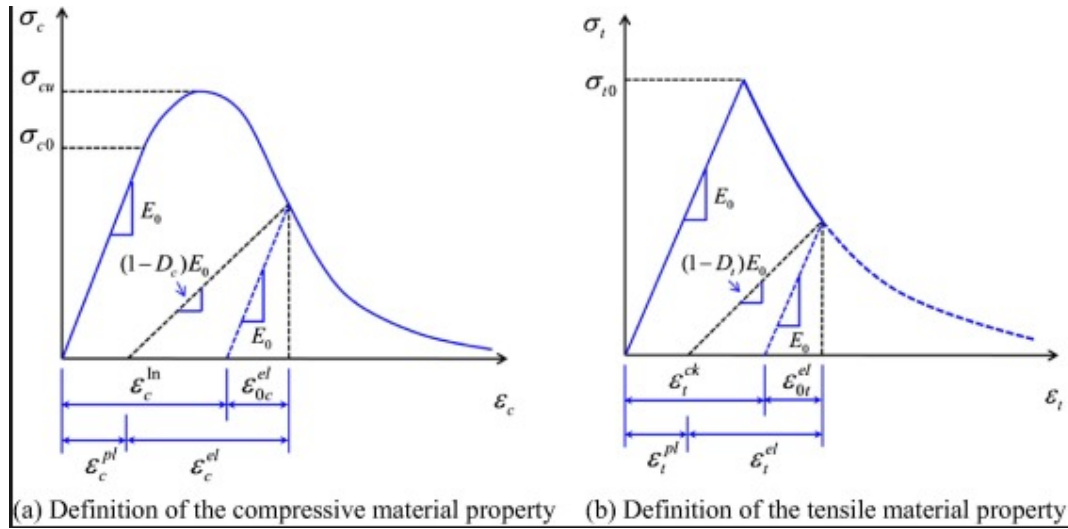


Figure 2. Concrete Damaged Plasticity Model

$$D = \frac{E}{E_0} \quad (3)$$

Where,  $D$  is the damage parameter of concrete in compression and tension,  $E_0$  is the initial (undamaged) elastic stiffness of the material,  $E$  is the damaged elastic stiffness of the confined concrete and  $d_t$  and  $d_c$  are the damage indices of concrete in tension and compression. Eq. 3 was used in calculating the damage parameters under uni-axial tension and compression.

The approach used to model the effects of confinement of plain and steel fiber reinforced concrete was similar to the approach used by (Dai and Lam [14]). Figure 3 shows the equivalent uniaxial representation for the stress-strain curve of confined and unconfined concrete.  $f_c$  is the unconfined concrete cylindrical compressive strength which is equal to  $0.8f_{cu}$ ; where  $f_{cu}$  is the cube compressive strength of the unconfined concrete. The unconfined strain ( $\epsilon_c$ ) value is taken as 0.003 for plain concrete as recommended by the ACI Specification (ACI [15]).  $f_{cc}$  and  $\epsilon_{cc}$  are the confined concrete compressive strength and confined strain, respectively. As described by Mander et al. [16].

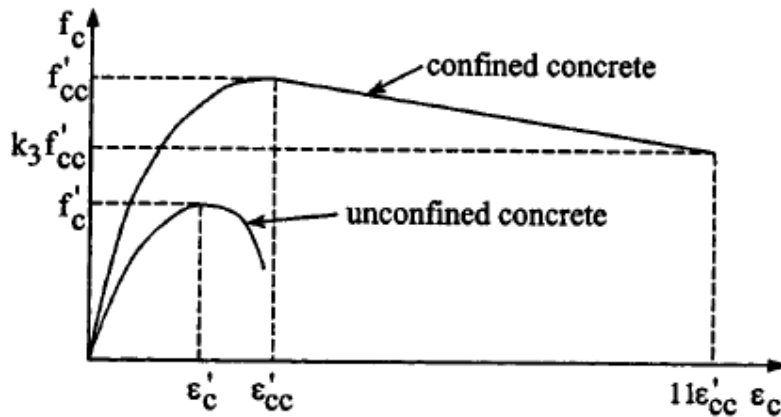


Figure 3. Confined Concrete Stress-strain Curve

$$f_{cc} = f_c + k_1 f_l \quad (4)$$

$$\varepsilon_{cc} = \varepsilon_c \left( 1 + k_2 \frac{f_l}{f_c} \right) \quad (5)$$

Where  $f_l$  = lateral confining pressure from the steel tube section.

$$f_l = \frac{2\sigma\theta t}{D} \quad (6)$$

Where  $\sigma\theta = 0.1 f_y$  proposed by Mander et.al. [16].

The factors  $k_1$  and  $k_2$  in Eqs. 4 and 5 are taken as 4.1 and 20.5 respectively, as given by Richart, Brandzaeg and Brown [17].

The equivalent stress–strain curves of unconfined and confined concrete are expressed in three parts. The first part defines the initial limit stress, which is taken as  $0.5 f_{cc}$  as given by Hu et al. [18]. The Young's modulus of confined concrete is calculated using the empirical formula provided in the ACI code [15], given in Eq. 7.

$$E_{cc} = 4700 \sqrt{f_{cc}} \text{ Mpa} \quad (7)$$

Where  $f_{cc}$  is the strength of confined concrete. The Poisson's ratio of confined concrete is taken as 0.2 as given in EN 1992-1-1 [19]. The second part defines the nonlinear portion of the stress-strain curve starting from the proportional limit stress  $0.5 f_{cc}$  to the confined strength of the concrete  $f_{cc}$ . This part of the curve was proposed by Saenz [20] and can be determined from Eq. 8.

$$f = \frac{E_c \varepsilon_c}{1 + (R + R_E - 2) \left( \frac{\varepsilon}{\varepsilon_{cc}} \right) - (2R - 1) \left( \frac{\varepsilon}{\varepsilon_{cc}} \right)^2 + R \left( \frac{\varepsilon}{\varepsilon_{cc}} \right)^2} \quad (8)$$

$$R_E = \frac{E_{cc} \varepsilon_{cc}}{f_{cc}} \quad (9)$$

$$R = \frac{R_E (R_\sigma - 1)}{(R_\sigma - 1)^2} - \frac{1}{R_\sigma} \quad (10)$$

Where the constants  $R_\sigma$  and  $R_\varepsilon$  are equal to 4 as recommended by Hu and Schnobrich [21].

The third part defines the descending value of the confined concrete stress–strain curve; this part starts from the maximum confined concrete strength  $f_{cc}$  to a lower value  $rk_{3c} f_{cc}$  with a corresponding strain value of  $11\varepsilon_{cc}$  as proposed by Hu et al. [18].

## 2.6 Material Modelling of Steel Fiber

The steel fiber dosage used in the model was a 0.75% volume (58.88 kg/m<sup>3</sup>) as described in the experimental tests. Table 2 shows the material geometry of the steel fiber is given in Musmar [22], Eq. 11 to determine the value of the tensile strength of the concrete.

Table 2. Steel Fibre Geometry					
S.F Type	Density kg/m <sup>3</sup>	%volume	Dosage (kg/m <sup>3</sup> )	Length mm	Diameter mm
Hooked End	7850	0.75%	58.88	35	0.55

$$f_{sp} = \left( 0.6 + 0.4 \left( v_f \times \frac{L_f}{d} \right) \right) \times \sqrt{f_c} \quad (11)$$

Where  $f_{sp}$  is the concrete tensile strength in MPa,  $v_f$  is the fiber volume,  $L_f$  = length of fiber,  $d$  = diameter of fiber and  $f_c$  is the compressive strength of concrete.

## 2.7 Concrete – Steel Tube Interface

Contact between the steel and concrete were modelled as a general contact. Friction between the two faces is maintained throughout when in contact. After conducting a parametric study for the coefficient of friction, 0.2 was chosen as it gave the best match for friction between the steel tube and concrete surfaces.

## 3. RESULTS AND DISCUSSION

The ultimate axial load and moment values for each column were reported in Table 3. Figure 4 shows the graphical plot of force vs B/t ratio, while Figure 5 shows graphical plot of moment vs B/t ratio for plain and steel fibre reinforced concrete infill for the CFST columns. It can be seen that the use of steel fibre reinforced concrete infill had little effect on the ultimate strength of the column. The steel tube thickness and load eccentricity are important factor which governed the ductility and ultimate strength of the columns.

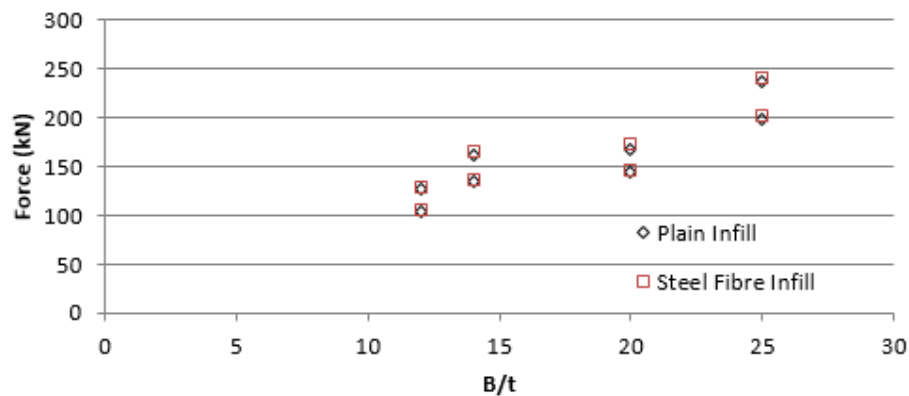


Figure 4. Force vs B/t Ratio

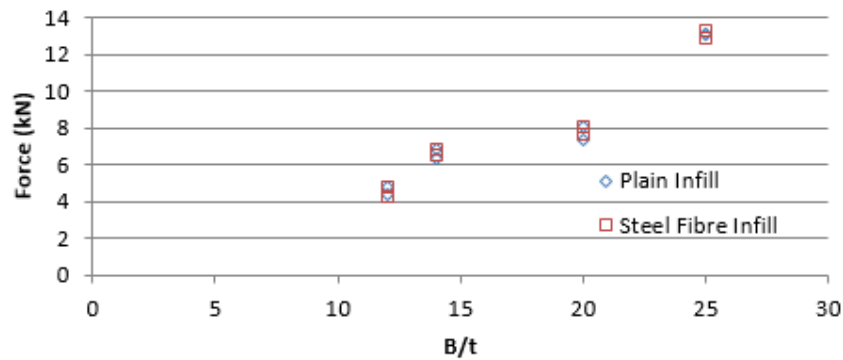


Figure 5. Moment vs B/t Ratio

Table 3. Finite Element Analysis Result

Model No.	Pp (kN)	PSF (kN)	MP (kN.m)	MSF (kN.m)
S60-5-30-290	126.6	128.1	4.36	4.3
S60-5-40-290	104.7	105.8	4.78	4.83
S70-5-35-290	161.3	164.8	6.31	6.57
S70-5-45-290	134.4	137.2	6.86	6.89
S80-4-40-290	167.8	173.8	7.39	7.72
S80-4-50-290	144.6	146.3	8.04	8.04
S100-4-50-290	237.5	239.9	13.06	12.88
S100-4-60-290	198.2	201.6	13.15	13.27

#### 4. PARAMETRIC STUDY

Prior to a sensitivity analysis, The FEA results were validated with the laboratory experiments which is discussed extensively in the next section. The parameters investigated includes; the steel tube thickness, concrete compressive strength, e/D ratio and steel tube yield strength. Table 4 shows the result obtained from the parametric study.

Table 4. CFST Parametric Study

Model No.	PP (kN)	PSF (kN)	fy (MPa)	B/t
S100-4-0-290	826.9	867.3	290	25
S100-6-0-290	1006	1038.17	290	16.67
S100-4-0-350	927.3	963.6	350	25
S100-6-0-350	1147	1182	350	16.67
S100-4-25-290	364.6	401.3	290	25
S100-6-25-290	468	517.13	290	16.67
S100-4-25-350	408	449.1	350	25
S100-6-25-350	524.7	577.5	350	16.67
S100-4-50-290	237.5	239.9	290	25
S100-6-50-290	311.2	317	290	16.67
S100-4-50-350	269.8	276.7	350	25
S100-6-50-350	354.9	353.8	350	16.67



#### 4.1 Steel Tube Thickness

For an increase in steel tube thickness from 4mm to 6mm there was a 21% increase in ultimate strength for columns loaded under compression only. For columns loaded with combined compression and bending, the increase recorded was about 32%. Figure 6 shows the steel tube thickness has a significant effect on the ductility of the columns. For columns having a depth over thickness ( $D/t$ ) ratio greater than 18 and eccentricity over depth ( $e/D$ ) ratio greater than 0.5, there was an uneven stress distribution during the early stages of load application which resulted in a premature plastic deformation at the top of the steel tube perpendicular to the eccentric load direction.

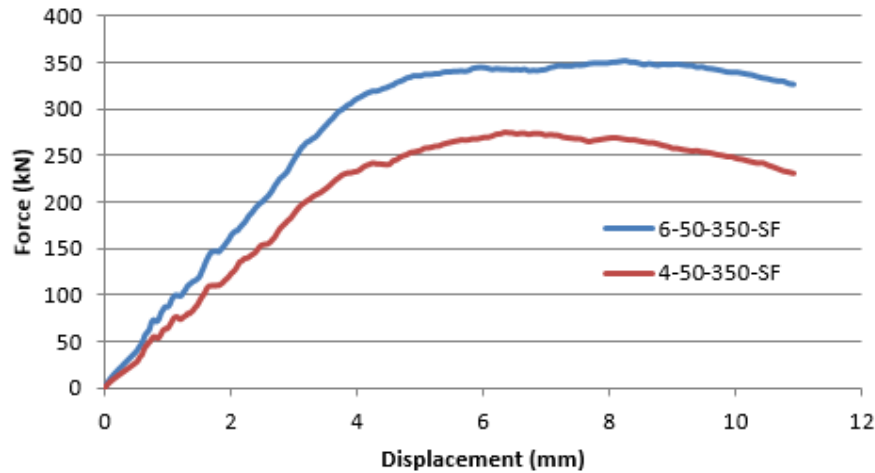
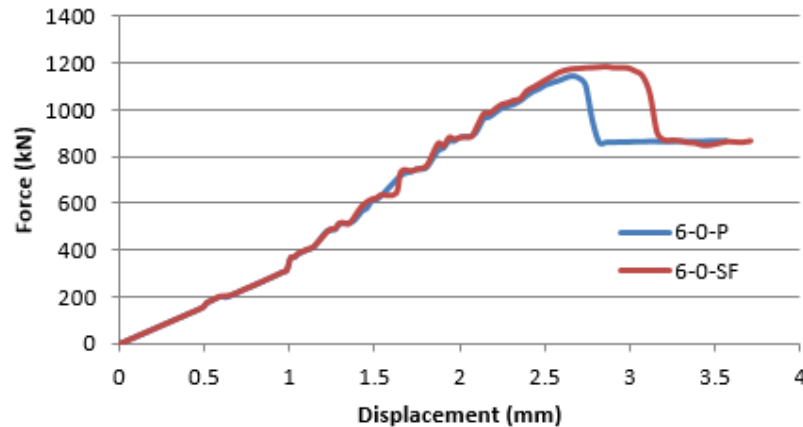


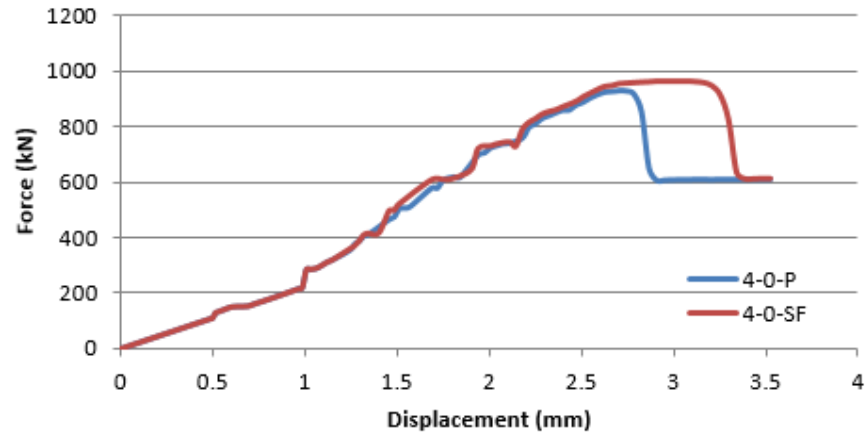
Figure 6. Steel Tube Thickness Effectiveness

#### 4.2 Concrete Compressive Strength

The concrete compressive strength had little effect on the ultimate strength value recorded for each column due to the slenderness of the column. Figures 7 (a) and 7(b) shows columns filled with steel fibre reinforced concrete (SFRC) and plain concrete. The SFRC columns maintained its ultimate strength value for a longer time period and therefore, gave the column a better ductility. For columns filled with plain concrete, there was a sudden drop in the strength of the columns. Figures 8(a) and 8(b) shows columns subjected to combine bending and compression, it was observed that columns filled with steel fibre reinforced concrete maintained 85% of its axial strength while the displacement increased.

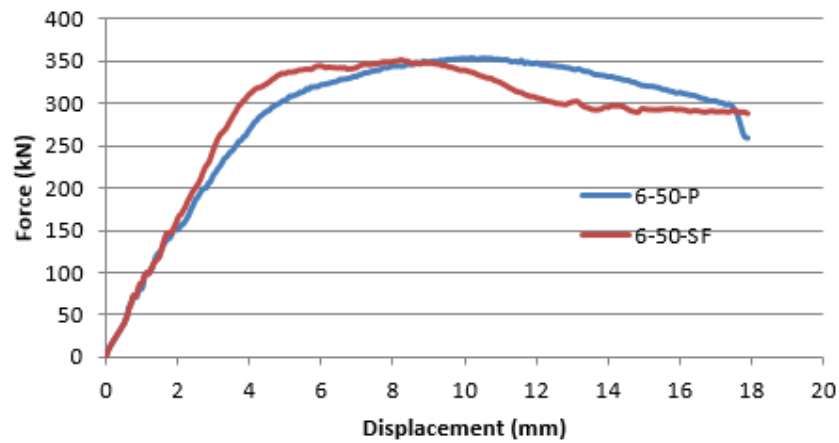


(a) 6 mm steel tube thickness

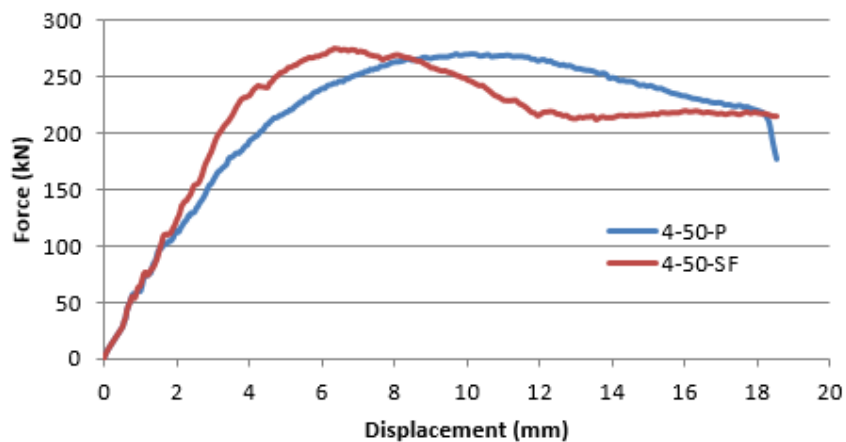


(b) 4 mm steel tube thickness

Figure 7. Effectiveness of Concrete Compressive Strength under Compression Only



(a) 6 mm steel tube thickness

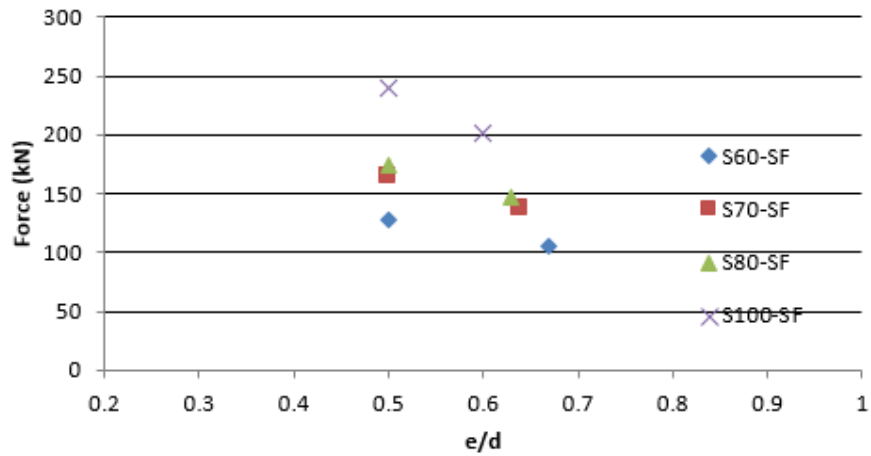


(b) 4 mm steel tube thickness

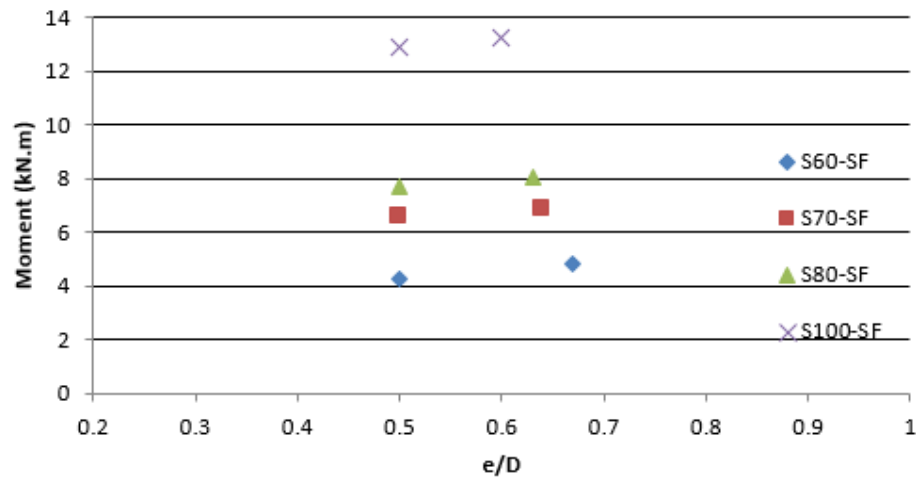
Figure 8. Effectiveness of Concrete Compressive Strength under Combine Bending and Compression

### 4.3 Load Eccentricity

The  $e/D$  ratio of the column was a contributing factor to the ultimate strength and moment values recorded. Figure 9 (a) shows for a 10mm increase in eccentric load distance of the columns, there was an average of 20% decrease in the ultimate strength value recorded for all CFST columns, however, the moment values recorded were not significantly affected. Figure 9 (b) shows there was an average of 6% increase in moment value recorded, with a 10mm increase in the eccentric load distance of the applied axial load.



(a) Force Vs e/D ratio



b) Moment Vs e/D ratio

Figure 9. Effectiveness of  $e/D$  Ratio of the Column

### 4.4 Steel Tube Yield Strength

The steel tube yield strength contributed significantly to the ultimate axial strength, but did not affect the ductility of the column. For a 20% increase in the steel tube yield strength there was a corresponding 14% increase in the axial strength of the column. Figure 10 shows the load deflection curve comparison of columns having similar geometries, but different steel tube yield strength.

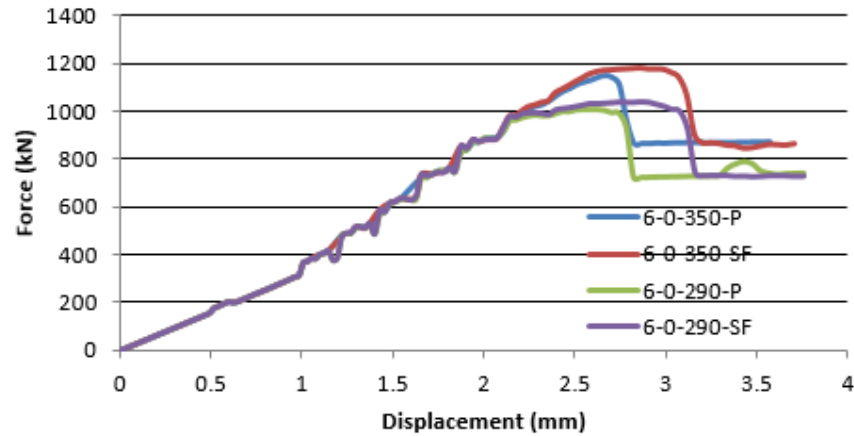
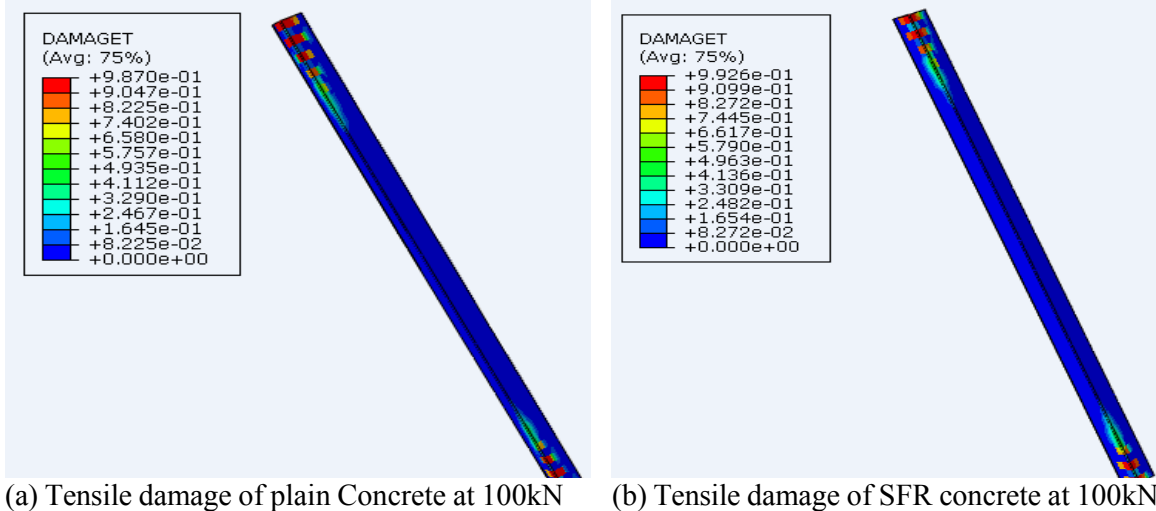


Figure 10. Steel Tube Yield Strength Effectiveness

#### 4.5 Concrete Infill Type

The addition of steel fibre to the concrete increases the tensile strength of the concrete and also controls the crack width propagation of the column. For columns filled with steel fibre reinforced concrete, the tensile damage of the concrete was relatively low compared to columns filled with plain concrete and this affected the crack propagation and ductility of the column. Figures 11(a) and (b) shows the concrete tensile damage for S60-5-30-290-I-P and S60-5-30-290-II-SF respectively, when a load of 100kN was applied to the column.



(a) Tensile damage of plain Concrete at 100kN

(b) Tensile damage of SFR concrete at 100kN

Figure 11. Effectiveness of Concrete Infill

### 5. COMPARISON OF FINITE ELEMENT ANALYSIS WITH LABORATORY EXPERIMENT AND EUROCODE 4 DESIGN GUIDE

There was good correlation between recorded values obtained from the numerical analysis when compared to the experimental and Eurocode 4 values. The axial compressive strength known as the squash load of a tubular column is calculated by adding the strength of its members as given in Eurocode 4 Part 1-1. A further calculation needs to be carried out when the column is loaded under combined compression and bending. The ultimate axial strength obtained from the finite element

(PFEA) analysis, laboratory experiments (PEXP) and Eurocode 4 calculations (PEC4) are reported in Table 5. The squash load for a fully encased concrete filled steel tube column according to Eurocode 4 is calculated using Eq. 12. Figures 12(a) and (b) shows the plot of force vs moment, while Figures 13 (a) to (d) shows the load deflection curve comparison for the laboratory experiments and FEA.

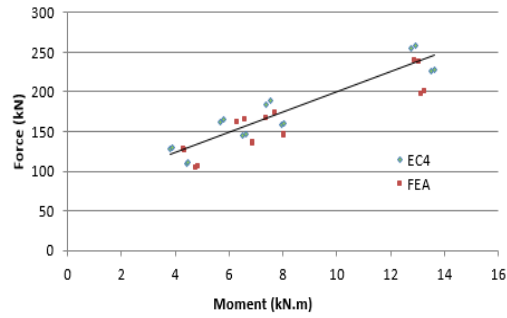
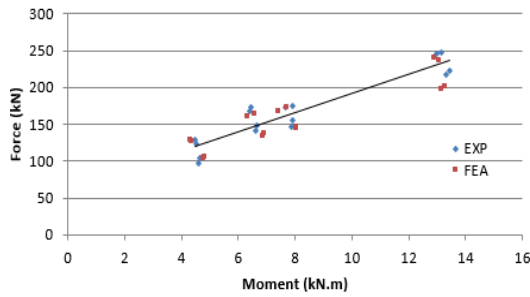
$$P_{EC4} = A_a f_y + A_c f_c \quad (12)$$

Where  $f_y$  is the yield strength of the structural steel,  $f_c$  is the cylindrical compressive strength of concrete.  $A_a$  and  $A_c$  are the area of steel and concrete respectively.

The moment (M) of the column at mid-height was calculated using the equation  $M = P \times (e + d_m)$  where P is the ultimate load, e is the eccentric distance and  $d_m$  is the deflection of the column at mid-height.

Table 5. Finite Element Analysis, Laboratory Experiments and Eurocode 4 Comparison

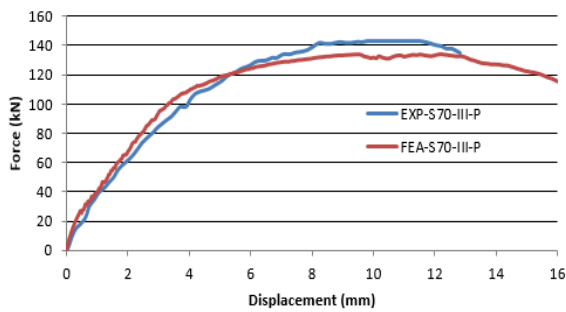
Model No.	P <sub>FEA</sub> kN	P <sub>EXP</sub> kN	P <sub>EC4</sub> kN	M <sub>FEA</sub> kN.m	M <sub>EXP</sub> kN.m	M <sub>EC4</sub> kN.m	$\frac{P_{EXP}}{P_{FEA}}$	$\frac{P_{EC4}}{P_{FEA}}$	$\frac{M_{EXP}}{M_{FEA}}$	$\frac{M_{EC4}}{M_{FEA}}$
S60-5-30-290-I-P	126.6	128	127.6	4.36	4.48	3.83	1.01	1.01	1.03	0.88
S60-5-30-290-II-SF	128.1	124	129.7	4.3	4.5	3.89	0.97	1.01	1.05	0.91
S60-5-40-290-III-P	104.7	97	110.3	4.78	4.6	4.42	0.93	1.05	0.96	0.92
S60-5-40-290-IV-SF	105.8	104	112	4.83	4.63	4.48	0.98	1.06	0.96	0.93
S70-5-35-290-I-P	161.3	168	162.6	6.31	6.41	5.69	1.04	1.01	1.02	0.90
S70-5-35-290-II-SF	164.8	174	165.7	6.57	6.46	5.80	1.06	1.01	0.98	0.88
S70-5-45-290-III-P	134.4	142	144.8	6.86	6.61	6.52	1.06	1.08	0.96	0.95
S70-5-45-290-IV-SF	137.2	148	147.1	6.89	6.65	6.62	1.08	1.07	0.97	0.96
S80-4-40-290-I-P	167.8	173	184.5	7.39	7.65	7.38	1.03	1.10	1.04	1.00
S80-4-40-290-II-SF	173.8	175	189	7.72	7.9	7.56	1.01	1.09	1.02	0.98
S80-4-50-290-III-P	144.6	147	158.8	8.04	7.87	7.94	1.02	1.10	0.98	0.99
S80-4-50-290-IV-SF	146.3	156	160.5	8.04	7.92	8.02	1.07	1.10	0.99	1.00
S100-4-50-290-I-P	237.5	245	255.2	13.06	12.99	12.76	1.03	1.07	0.99	0.98
S100-4-50-290-II-SF	239.9	248	258.9	12.88	13.13	12.95	1.03	1.08	1.02	1.01
S100-4-60-290-III-P	198.2	218	225.6	13.15	13.33	13.53	1.10	1.14	1.01	1.03
S100-4-60-290-IV-SF	201.6	222	227.2	13.27	13.44	13.63	1.10	1.13	1.01	1.03
<b>Mean</b>							<b>1.03</b>	<b>1.07</b>	<b>1.00</b>	<b>0.96</b>
<b>Standard Deviation</b>							<b>0.05</b>	<b>0.04</b>	<b>0.03</b>	<b>0.05</b>



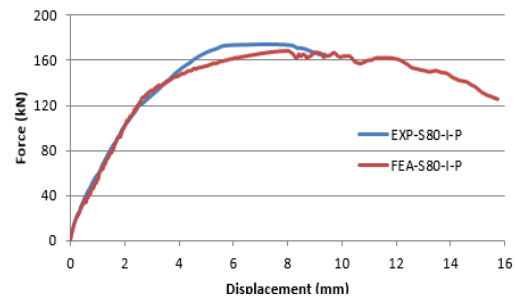
(a) Comparison of FEA with experiment

(b) Comparison of FEA with Eurocode 4

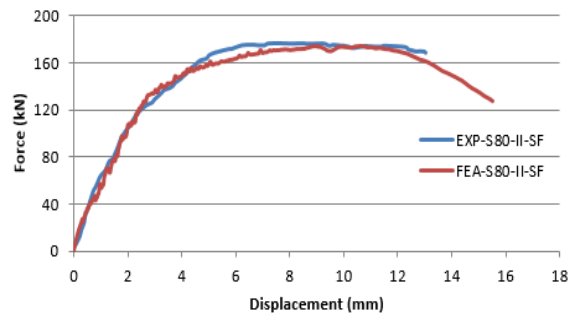
Figure 12. Force vs Moment Plot Comparison



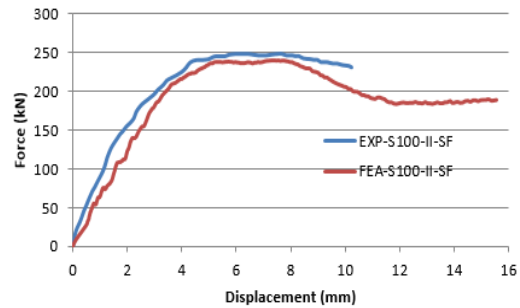
(a) Force vs Displacement



(b) Force vs Displacement



(c) Force vs Displacement



(d) Force vs Displacement

Figure 13. Force vs Displacement Curve FEA and Laboratory Experiment Comparison

## 6. CONCLUSIONS

The computational finite element modelling of concrete filled steel tubular column with plain and steel fiber reinforced concrete infill is presented in this study. There was a good agreement between ultimate strength and moment values of the columns when compared to values obtained from experimental data and Eurocode 4 Part 1-1.

Addition of steel fiber to the concrete had little effect on the ultimate strength of the column. However, this affected the ductility and crack width propagation of the column and also increased the concrete tensile strength. This indicates that for CFST columns filled with steel fiber reinforced concrete, the column will have a higher ductility when compared to using a plain concrete infill. The steel tube yield strength had an effect on the ultimate axial strength of the column; however, it did not contribute to the ductility of the column. It is recommended to increase the steel tube thickness rather than using a steel tube section with a higher yield strength for design purposes. Using an  $e/D$  ratio less than 0.5 for the construction of slender columns is recommended so as to utilize the full section of the column when loaded axially.

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