

# STATIC BEHAVIOR OF AXIALLY COMPRESSED CIRCULAR CONCRETE FILLED CFRP-STEEL TUBULAR (C-CF-CFRP-ST) COLUMNS WITH MODERATE SLENDERNESS RATIO

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**ABSTRACT:** Thirty-two specimens are experimentally tested in this paper to study the static performance of axially compressed circular concrete filled CFRP-steel tubular (C-CF-CFRP-ST) columns. The tested results indicate that, for columns with relative small slenderness ratio, failure is dominated by the strength loss of the materials. However, for columns with relative large slenderness ratio, failure is controlled by instability. The load versus deflection curves at the mid-height of the composite column can be divided into three stages, i.e., elastic, elasto-plastic and softening stage. Analyses of the tested results show that distribution of longitudinal strains in the steel tube over depth on the cross-section is approximately linear, and the steel tube and its outer CFRP material can cooperate both longitudinally and transversely. The longitudinal strain and the transverse strain at a point have opposite signs, and the steel tube under longitudinal tension has no transverse confinement effect on its concrete. The Deformed modes of the columns, the axial load versus deflection curves at the mid-height, the axial load versus axial shortening curves and the stresses in the steel tube are simulated by using finite element method. The calculated results agree well with the experimental results to prove the accuracy of the finite element model. Stresses in the concrete, the steel tube and the CFRPs are analyzed by using finite element method. The numerical results show that the interaction force between the steel tube and the concrete decreases gradually from compressive region to tensile region. The adhesive strength between the concrete and the steel tube has little effect on the critical buckling load and on the elastic stiffness of the columns. Equation for calculating the critical buckling load of the composite columns is presented, and the estimated results agree well with the experimental results.

**Keywords:** Circular CFRP-steel tube, In-filled concrete, Axially compressed columns with moderate slenderness ratio, Static performance, Critical buckling load

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## 1. INTRODUCTION

Fiber Reinforced Plastic (FRP) has been used in many engineering structures due to its advantages of high strength/weight ratio, good corrosion resistance, ease of installation, more and more cheaper cost and so on, in which Concrete Filled FRP Tubular (CF-FRP-T) structure or FRP strengthened concrete structure is a typical example. There are many research reports on CF-FRP-T (Wang and Restrepo [1]; Fam and Rizkalla [2]; Teng et al. [3]; Karabinis et al. [4]; Rousakis et al. [5]; Yu. et al. [6]; Yu. et al. [7]; Jiang and Wu [8]). CF-FRP-T structures have better corrosion resistance. However, the failure mode of CF-FRP-T structures has brittle characteristics in most cases, and the load carrying capacity in the transverse direction for this structure is weak.

As one typical style of the steel-concrete composite structures, Concrete Filled Steel Tubular (CFST) structures are widely used in civil engineering, and they show good constructional efficiency. The research work in this field has been studied systematically in the literature. Besides the systematic investigations on the static and the hysteretic behavior of the components and the connections (Han [9]; Han et al. [10]; Han et al. [11]; Han et al. [12]; Han and Li [13]), fire resistance (Han [14]), torsion performance (Han et al. [15]) and local compression (Han et al. [16])

of this structure are also reported. Comparing with the CF-FRP-T, CFST has higher shearing load carrying capacity. However, the outer surface corrosion of the steel tube cannot be ignored when CFST is used in a corrosive environment, and some corresponding research studies in this field have been reported in recent years (Han et al. [17]; Han et al. [18]).

In many engineering fields, the FRP-metal composite tanks or tubes have been used widely, such as gas tank used in motor vehicle (as shown in Figure 1, where GFRP refers to Glass Fiber Reinforced Plastic) and pipeline system for transporting high pressure gas or liquid used in municipal engineering or chemical engineering. Sometimes, petroleum pipeline system after corrosion is also reinforced with CFRP (Carbon Fiber Reinforced Plastic), which can save much cost compared to the measure of replacing the corroded tube with a new one. CFRP-metal tube can also be used in civil engineering, for example, by infilling concrete into CFRP-steel composite tube (Che et al. [19]), or by using CFRP to strengthen damaged CFST (Tao et al. [20]). Both of the above methods can form the so-called Concrete Filled CFRP-Steel Tubular (CF-CFRP-ST) structures. CF-CFRP-ST structures have the advantages of both the CFST and the CF-FRP-T structures, and the CF-CFRP-ST structures can also avoid the respective deficiency of the CFST and the CF-FRP-T structures to some degree. Recent study shows that CF-CFRP-ST has satisfactory fire endurance time when adequate fire resistant measures have been taken (Tao et al [21]).



Figure 1. Gas Tank Used in Motor Vehicle



Figure 2. An Engineering Practice of C-CF-CFRP-ST Columns Used in Nanjing City, Jiangsu Province, P. R. China

There are many research studies about CF-CFRP-ST structures in the literature, and these studies mostly focus on Circular CF-CFRP-ST (C-CF-CFRP-ST) stub columns (Xiao et al. [22]; Choi and Xiao [23]; Park et al. [24]; Hu et al. [25]; Li et al. [26]; Teng et al. [27]), C-CF-CFRP-ST flexural members (Wang and Shao [28]), Square CF-CFRP-ST (S-CF-CFRP-ST) stub columns (Tao et al

[29]; Park et al. [30]; Sundararaja and Ganesh [31]; Sundararaja and Ganesh [32]; Sundararaja and Ganesh [33]; Wang and Shao [34]) and S-CF-CFRP-ST flexural members (Sundararaja and Ganesh [35]; Wang et al. [36]). More applications in practical engineering are columns with large slenderness ratio (as shown in Figure 2) although corresponding research is quite scarce. For axially compressed stub columns (slenderness ratio  $\lambda \leq 3$ ), compressive buckling does not occur in general, and its load carrying capacity is determined by the material properties and the combination effect, while for axially compressed columns with moderate slenderness ratio, i. e.,  $\lambda > 3$ , its critical buckling load is generally determined by stability, which is necessary to be studied specially.

To understand the static performance of the axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio, 32 composite specimens with both transverse CFRP and longitudinal CFRP are tested and the details are introduced in this paper. Axial load ( $N$ ) versus deflection at the mid-height ( $u_m$ ) curves, cooperation between the steel tube and the CFRP and plane section assumption of the composite specimens are analyzed. Furthermore, the finite element software ABAQUS is used to simulate the deformed modes and the  $N-u_m$  curves of the composite columns. The distributions of the stress and the strain, the effects of adhesive strength between the steel tube and the concrete, and the interaction force ( $p$ ) between the concrete and the steel tube are also analyzed. Finally, the equation for calculating the critical buckling load of the axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio is given.

## 2. EXPERIMENTAL PROGRAM

### 2.1 General

In overall, tests on 32 axially compressed C-CF-CFRP-ST columns are conducted, and the basic parameters considered for these specimens include  $\lambda$  and strengthening factor of the longitudinal CFRP ( $\eta$ ) (Wang and Shao [28]), respectively, where

$$\lambda = 4L/D_s \quad (1)$$

$$\eta = A_{\text{cfl}} f_{\text{cfl}} / (A_s f_y) \quad (2)$$

$$f_{\text{cfl}} = E_{\text{cf}} \varepsilon_{\text{cflr}} = 2300 \text{MPa} \quad (3)$$

where  $L$  is the length of the column;  $D_s$  is the outer diameter of the steel tube.  $A_{\text{cfl}}$  and  $f_{\text{cfl}}$  are the cross-sectional area and the ultimate tensile strength of the longitudinal CFRP, respectively.  $A_s$  and  $f_y$  are the cross-sectional area and the yield strength of the steel tube, respectively.  $E_{\text{cf}}$  and  $\varepsilon_{\text{cflr}}$  are the elasticity modulus of CFRP and the rupture strain of the longitudinal CFRP, respectively. In this study,  $\varepsilon_{\text{cflr}} = 10000 \mu\epsilon$ , and the determination of  $\varepsilon_{\text{cflr}}$  can be referred to the corresponding reference (Wang and Shao [28]).

The specimens' details are provided in Table 1. In the nomenclature of the specimens as listed in Table 1, CC means Circular Column. Letters A, B, C, D, E, F, G and H denote the different lengths of the columns: 400mm, 530mm, 600mm, 800mm, 1200mm, 1800mm, 2400mm and 3000mm, respectively. Number 0, 1, 2 or 3 refers to the number of the longitudinal CFRP layer(s) ( $m'$ ).  $m$  is

number of the transverse CFRP layer.  $t_s$  is the wall thickness of the steel tube, and  $N_{u,cr}^t$  is the tested value of the critical buckling load of the C-CF-CFRP-ST columns.  $\xi_s$  is the confinement factor of the steel tube (Han [9]).  $\xi_{cf}$  is the confinement factor of the transverse CFRP tube (Che et al. [19]), where

$$\xi_s = A_s f_y / (A_c f_{ck}) \quad (4)$$

$$\xi_{cf} = A_{cft} f_{cft} / (A_c f_{ck}) \quad (5)$$

$$f_{ck} = 0.67 f_{cu} \quad (6)$$

$$f_{cft} = E_{cf} \varepsilon_{cfr} = 1265 \text{ MPa} \quad (7)$$

where  $A_c$  and  $f_{ck}$  are the cross-sectional area and the characteristic axial compressive strength of the concrete, respectively.  $A_{cft}$  and  $f_{cft}$  are the cross-sectional area and the ultimate tensile strength of the transverse CFRP, respectively.  $f_{cu}$  is the cubic strength of the concrete specimen.  $\varepsilon_{cfr}$  is the rupture strain of the transverse CFRP ( $\varepsilon_{cfr} = 5500 \mu\epsilon$ ) and the determination of  $\varepsilon_{cfr}$  can be referred to the corresponding reference (Che et al. [19]).

## 2.2 Specimen Preparations

Fabrication of Circular CFST (C-CFST) specimens can be found in relative reference (Han [9]). Carbon fiber sheets are applied using a hand lay-up method. The longitudinal CFRP is glued firstly, and then the transverse CFRP is glued. The finishing end of a sheet is overlapped to the starting end of the other sheet with an overlapped length of 150 mm.

Table 1. Specimen Labels and Capacities

No.	Specimens label	$L$ (mm)	$\lambda$	$m'$ (layer(s))	$\eta$	$m$ (layer)	$\xi_{cf}$	$D_s$ (mm)	$t_s$ (mm)	$\xi_s$	$N_{u,cr}^t$ (kN)
1	CC A-0	400	12	0	0	1	0.13	133	5	1.3	2085
2	CC A-1	400	12	1	0.18	1	0.13	133	5	1.3	2118
3	CC A-2	400	12	2	0.35	1	0.13	133	5	1.3	2119
4	CC A-3	400	12	3	0.53	1	0.13	133	5	1.3	2206
5	CC B-0	530	16	0	0	1	0.13	133	5	1.3	2040
6	CC B-1	530	16	1	0.18	1	0.13	133	5	1.3	1947
7	CC B-2	530	16	2	0.35	1	0.13	133	5	1.3	2016
8	CC B-3	530	16	3	0.53	1	0.13	133	5	1.3	2094
9	CC C-0	600	18	0	0	1	0.13	133	4.5	1.3	1721
10	CC C-1	600	18	1	0.18	1	0.13	133	4.5	1.3	1756
11	CC C-2	600	18	2	0.35	1	0.13	133	4.5	1.3	1831
12	CC C-3	600	18	3	0.53	1	0.13	133	5	1.3	2090
13	CC D-0	800	24	0	0	1	0.13	133	4.5	1.3	1682

14	CC D-1	800	24	1	0.18	1	0.13	133	4.5	1.3	1724
15	CC D-2	800	24	2	0.35	1	0.13	133	4.5	1.3	1780
16	CC D-3	800	24	1	0.53	1	0.13	133	5	1.3	2035
17	CC E-0	1200	36	2	0	1	0.13	133	4.5	1.3	1445
18	CC E-1	1200	36	1	0.18	1	0.13	133	4.5	1.3	1500
19	CC E-2	1200	36	2	0.35	1	0.13	133	4.5	1.3	1560
20	CC E-3	1200	36	3	0.53	1	0.13	133	5	1.3	1914
21	CC F-0	1800	54	0	0	1	0.13	133	4.5	1.3	1222
22	CC F-1	1800	54	1	0.18	1	0.13	133	4.5	1.3	1281
23	CC F-2	1800	54	2	0.35	1	0.13	133	4.5	1.3	1358
24	CC F-3	1800	54	3	0.53	1	0.13	133	5	1.3	1704
25	CC G-0	2400	72	0	0	1	0.13	133	5	1.3	1387
26	CC G-1	2400	72	1	0.18	1	0.13	133	5	1.3	1409
27	CC G-2	2400	72	2	0.35	1	0.13	133	5	1.3	1428
28	CC G-3	2400	72	3	0.53	1	0.13	133	5	1.3	1613
29	CC H-0	3000	90	0	0	1	0.13	133	5	1.3	1296
30	CC H-1	3000	90	1	0.18	1	0.13	133	5	1.3	1174
31	CC H-2	3000	90	2	0.35	1	0.13	133	5	1.3	1243
32	CC H-3	3000	90	3	0.53	1	0.13	133	5	1.3	1467

### 2.3 Material Properties

Seamless steel tube is in the columns. Tensile tests on steel coupons cut from the original steel tubes are conducted. The measured properties of the steel tubes obtained from these tests are given in Table 2, where  $E_s$  and  $\nu_s$  are the elasticity modulus and the Poisson's ratio of the steel tube, respectively.

Table 2. Material Properties of Steel Tube

$t_s$ (mm)	$E_s$ (GPa)	$f_y$ (MPa)	$\nu_s$
4.5	206	333	0.27
5	204	303	0.26

The in-filled concrete of all the specimens has same material property. In the concrete mixture, Portland cement is used, and the fine aggregate is silica-based sand. The coarse aggregate is limestone with a largest size of 20mm, and 1% (in weight) water reducing agent is added. The mixture proportions of the concrete are summarized in Table 3.

Table 3. Mixture Proportions of Concrete ( $\text{kg}\cdot\text{m}^{-3}$ )

Cement	Water	Sand	Course aggregate
485	150	703	1062

To determine the compressive strength of the in-filled concrete, six cubes with a side length of 150 mm are cast and cured in conditions similar to those of the related specimens. The averaged cubic

strength ( $f_{cu}$ ) at 28 days is 48.8 MPa. At the testing time (six months later due to the delay of the test program), the cubic strength of 57.4 MPa is achieved and is adopted in later FE simulation and calculation. Elasticity modulus of the concrete ( $E_c$ ) is 35.9 GPa.

Carbon fiber sheet used in the specimens is a kind of one-way sheet, and the properties of the CFRP determined from tensile tests of six flat coupons are given in Table 4, in which  $f_{cf}'$ ,  $\delta_{cf}$  and  $w_{cf}$  are the tensile strength, the elongation percentage and the density of the carbon fiber sheet, and  $t_{cf}$  is the thickness of one-layer carbon fiber sheet.

Table 4. Main Technical Properties of Carbon Fiber Sheets

Model number	$f_{cf}'$ (GPa)	$E_{cf}$ (GPa)	$\delta_{cf}$ (%)	$w_{cf}$ (g·m <sup>-2</sup> )	$t_{cf}$ (mm)
C200/200	4.83	230	2.1	200	0.111

It should be pointed out that the rupture strain of the coupon CFRP is 21000  $\mu\epsilon$  while the rupture strains of the longitudinal CFRP  $\epsilon_{cfr}=10000\mu\epsilon$  and that of the transverse CFRP  $\epsilon_{cfr}=5500\mu\epsilon$ . Such difference is possibly caused by different curvatures at CFPR positions, and the relative research (Yu et al. [37]) provided similar conclusion.

JGN-C, a typical kind of epoxy resin, which is produced by Building Science Research Institute of Liaoning Province of China and is used for building structures, is selected for adhering the CFRP to the steel tube. Another kind of epoxy resin, JGN-P, is used for gluing CFRPs together.

## 2.4 Test Setup and Instrumentation

The experimental test is carried out in the Structural Laboratory of Shenyang Jianzhu University, P. R. China. The critical buckling load of the specimen is predicted before the specimen is loaded: the transverse and the longitudinal CFRPs are simplified to equivalent steel tube, and then the critical buckling load can be calculated by using corresponding equations of C-CFST columns (Han et al. [11]). However, the equivalent steel tube besides longitudinal CFRP is not considered in calculating the confinement factor of the steel tube  $\xi_s$ .

The test setup is shown in Figure 3. The specimen is pinned at both ends. A instrument with a loading capacity of 5,000kN is used to apply axial compressive load  $N$ . The load is applied in many loading steps. In the elastic stage, each loading step is 1/10 of the estimated critical buckling load. When the applied load is about 60% of the estimated critical buckling load, the magnitude of the loading step is reduced to 1/15-1/20 of the estimated critical buckling load. After the deflection at the mid-height exceeds  $L/50$ , displacement control is used till the deflection at the mid-height reaches about  $L/25$ . The interval between two continuous loading steps is maintained for about 2 to 3 min.

As shown in Figure 3, 3-5 Linear Variable Differential Transformers (LVDTs) are placed in the bending plane with equal distance in the height direction according to different heights of the specimens to measure the lateral deflection. Simultaneously, two LVDTs are used to measure the longitudinal compression of the specimens. Overall, 11 strain gauges are glued on the surfaces of each steel tube and on the CFRP at the mid-height of the specimens respectively, as shown in Figure 4, where points 1-7 are the locations for measuring the longitudinal strains and points 1, 3, 5 and 8 are the locations for measuring the transverse strains.

The data is captured by Data Acquisition System U-CAM-70A, and the  $N-u_m$  curve is achieved simultaneously.



Figure 3. Test Arrangement (Specimen CC H-1)

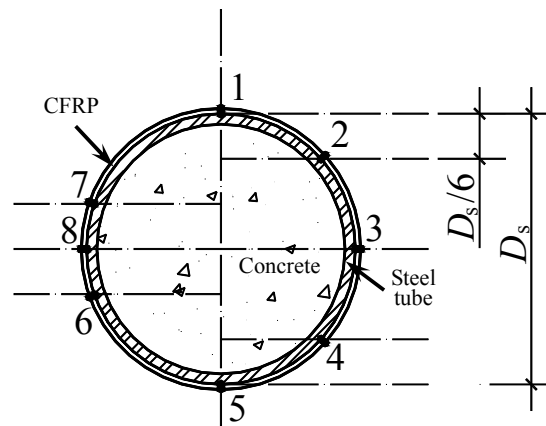


Figure 4. Location of Strain Gauges

## 2.5 Test Observations and Failure Modes

The failure of the specimens is mainly determined by the slenderness ratio ( $\lambda$ ). For specimens with small  $\lambda$ , transverse CFRP located in longitudinal compressive region at the mid-height begins to fracture at a loading about  $0.85 N_{u,cr}^t$ . With the increase of the applied load, the amount of fractured transverse CFFPs becomes bigger (as shown in Figure 5 (a)) till the applied load reaches  $N_{u,cr}^t$ . Longitudinal CFRP located in longitudinal tensile region at the mid-height is not fractured in general, and the specimens have local outward buckling (as shown in Figure 5 (a)) which indicates a symbol of strength failure. For specimens with large  $\lambda$ , transverse CFRP located in longitudinal compressive region at the mid-height begins to fracture after  $N_{u,cr}^t$ . With the increase of the deflection, the longitudinal CFRP located in longitudinal tensile region at the mid-height begins to fracture (as shown in Figure 5 (b)). Finally, the specimens fail and the steel tube does not buckle outward and forms an instability failure. All specimens after failure are shown in Figure 6.

The CFRP-steel composite tubes are cut off after test. As shown in Figure 7, it is found that the concrete could be divided into both tensile and compressive regions. For specimens with small  $\lambda$ ,



the failure of the concrete is severe, and the concrete in the compressive region is crushed (as shown in Figure 7 (a)). In the tensile region, the concrete crack has a big width, and the distance between any two adjacent cracks is small (as shown in Figure 7 (b)). For specimens with large  $\lambda$ , the concrete failure is not severe, and thus the concrete in compressive region is almost not damaged (as shown in Figure 7 (c)). The crack in tensile region has a narrow width, and the distance between any two adjacent cracks is bigger (as shown in Figure 7 (d)).

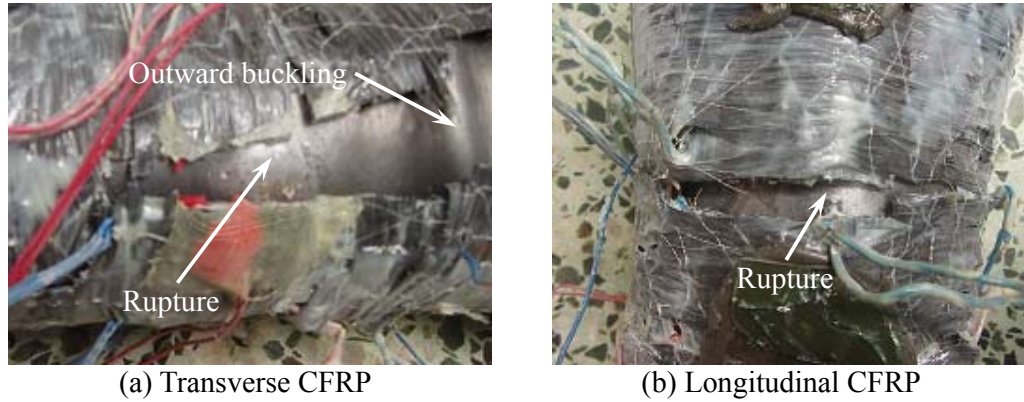


Figure 5. Rupture of CFRPs and Local Buckling



Figure 6. All Specimens after Testing

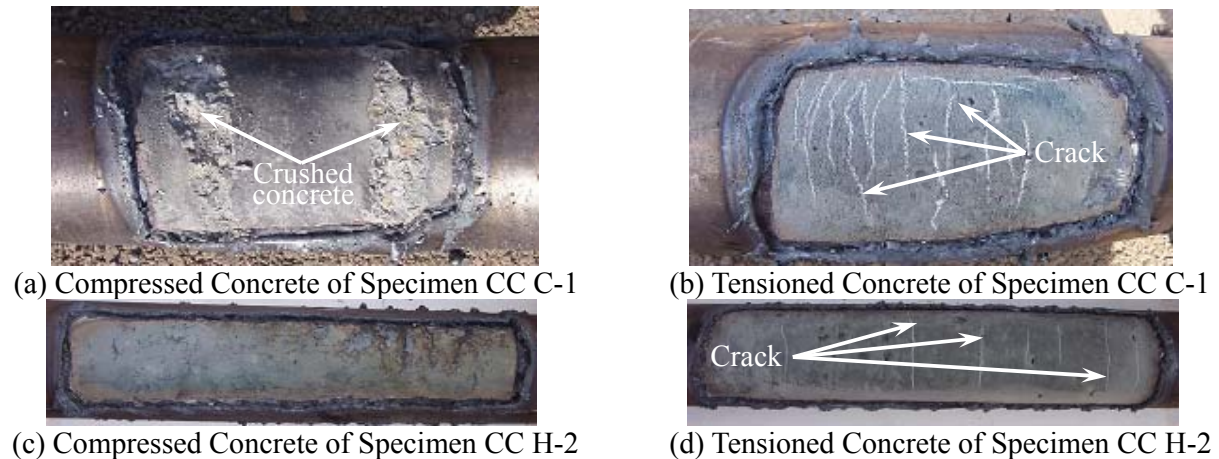


Figure 7. Failure Modes of Concrete

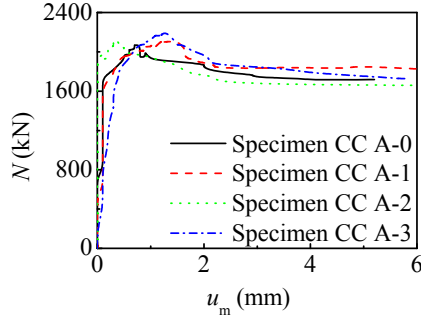
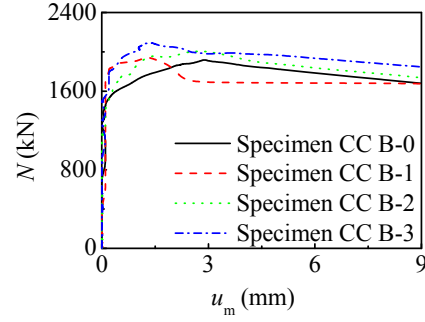
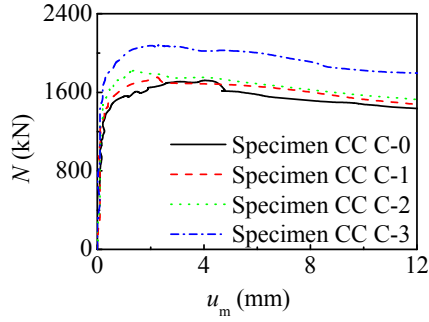
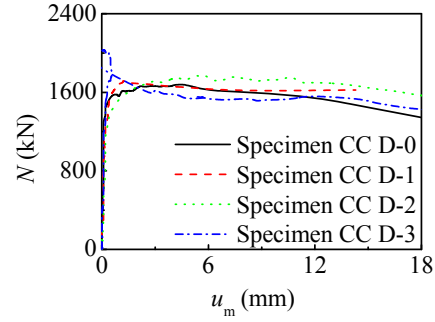
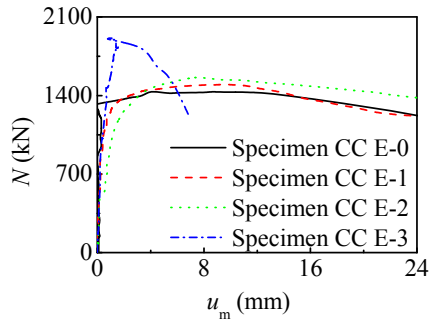
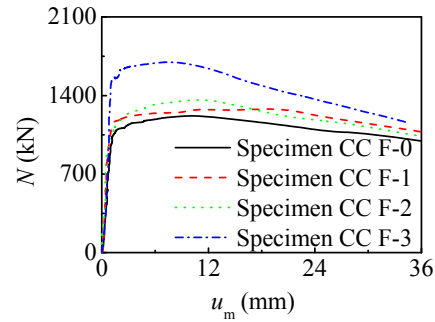
## 2.6 Test Results and Analysis

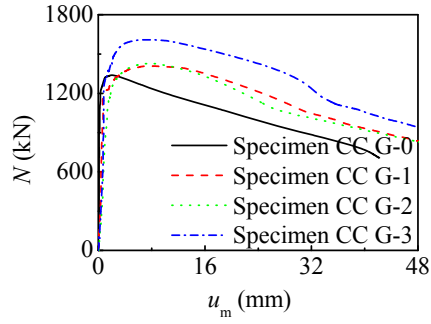
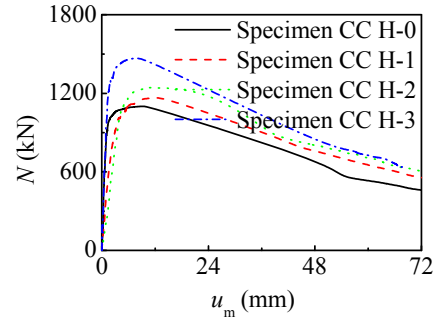
### 2.6.1 Tested $N-u_m$ curves

Figure 8 shows the  $N-u_m$  curves of the specimens, and it can be found that these  $N-u_m$  curves



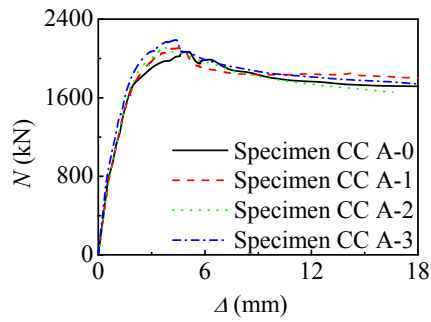
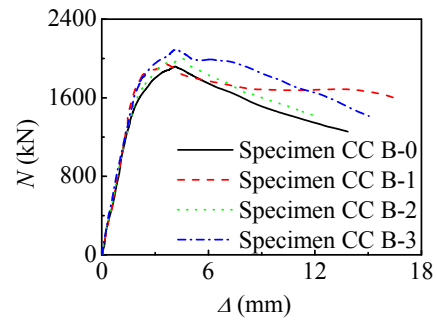
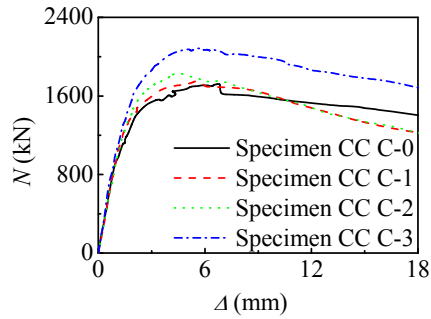
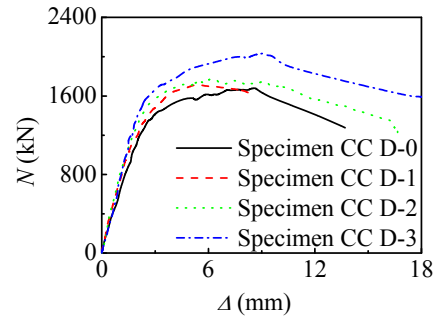
have the following characteristics: the curves develop linearly in initial loading stage, and this period belongs to an elastic stage. The following stage is elasto-plastic stage in which the developing rate of  $u_m$  is apparently faster than that of  $N$ . The curves begin to drop after  $N_{u,cr}^t$ , and in this stage the increase of  $u_m$  is much faster while the decrease of  $N$  is gradual.

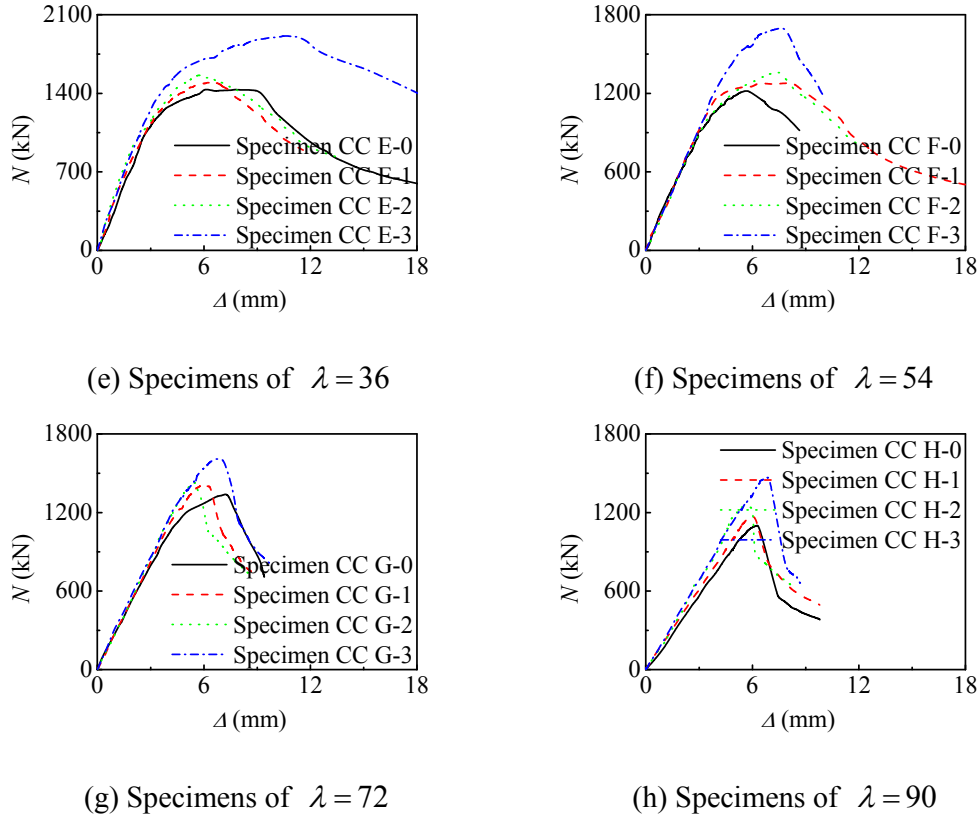
(a) Specimens of  $\lambda = 12$ (b) Specimens of  $\lambda = 16$ (c) Specimens of  $\lambda = 18$ (d) Specimens of  $\lambda = 24$ (e) Specimens of  $\lambda = 36$ (f) Specimens of  $\lambda = 54$

(g) Specimens of  $\lambda = 72$ (h) Specimens of  $\lambda = 90$ Figure 8. Tested  $N-u_m$  Curves

### 2.6.2 Tested $N-\Delta$ curves

Figure 9 shows the  $N-\Delta$  curves of the specimens, where  $\Delta$  is the axial shortening of the specimen.

(a) Specimens of  $\lambda = 12$ (b) Specimens of  $\lambda = 16$ (c) Specimens of  $\lambda = 18$ (d) Specimens of  $\lambda = 24$

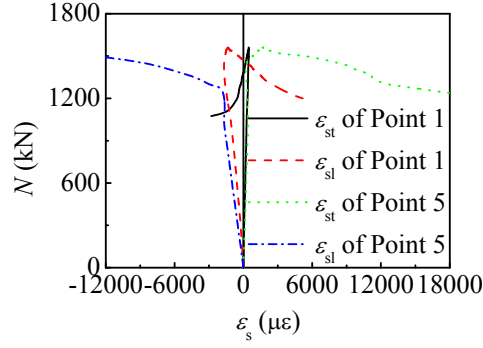
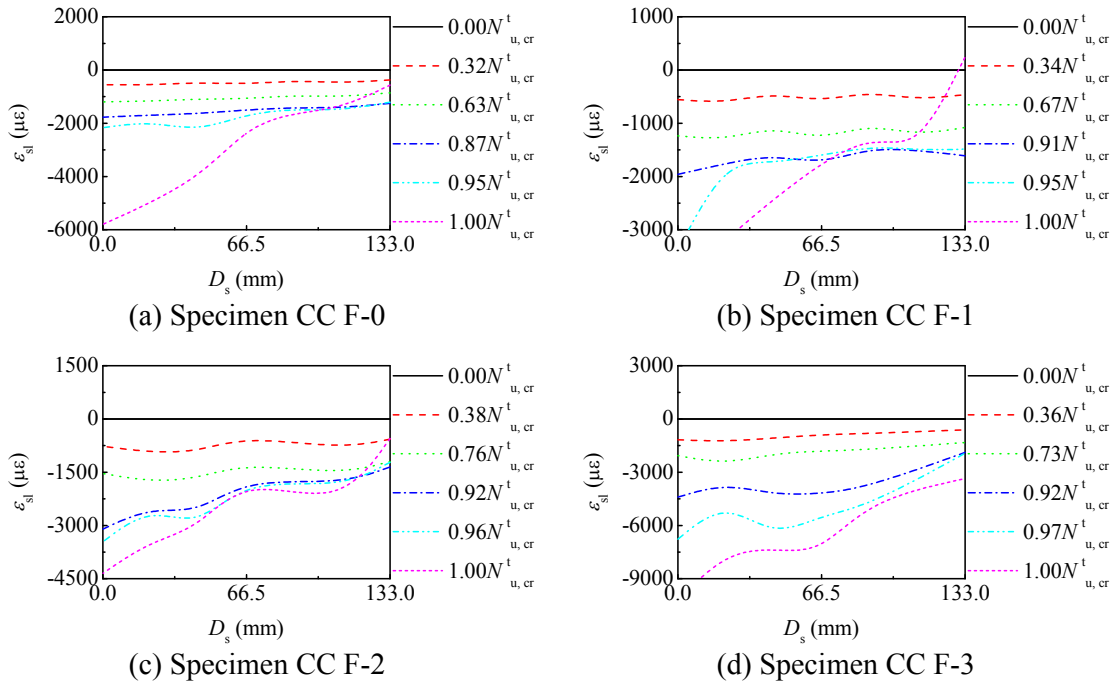
Figure 9. Tested  $N-\Delta$  Curves

### 2.6.3 Comparison between longitudinal Strain and Transverse Strain

Figure 10 shows comparison between  $\varepsilon_{sl}$  (longitudinal strain of the steel tube) and  $\varepsilon_{st}$  (transverse strain of the steel tube) at point 1 and point 5 for specimen CC E-2, where  $\varepsilon_s$  is the strain of the steel tube. The signs of  $\varepsilon_{sl}$  and  $\varepsilon_{st}$  at same point are different: it is negative in longitudinal direction while positive in transverse direction and vice versa. Studies on CF-CFRP-ST stub column (Che et al. [19]; Wang and Shao [34]) and CF-CFRP-ST flexural member (Wang and Shao [28]; Wang et al. [36]) provided same conclusions. It can also be found that point 1 on the steel tube is under tension longitudinally and under compression transversely after  $N_{u,cr}^t$ , which makes it clear that this point together with the around steel tube has no confinement to concrete, and the reason may be listed as follow: the nearby concrete is also in a tensile state when the steel tube is under tension in longitudinal direction, and thus it does not need transverse confinement provided from steel tube. The transverse strain of the steel tube is under compression due to the corresponding tension in longitudinal direction.

### 2.6.4 Plane Section Assumption

Figure 11 shows the distribution of  $\varepsilon_{sl}$  over the depth on the cross-section of the specimen with a slenderness ratio  $\lambda = 24$ . As shown in Figure 11, the distribution of  $\varepsilon_{sl}$  is basically satisfied with the plane section assumption. Studies on CF-CFRP-ST flexural member (Wang and Shao [28]; Wang et al. [36]) provided same conclusions.

Figure 10. Comparisons between  $\varepsilon_{sl}$  and  $\varepsilon_{st}$  of Point 1 and Point 5 for Specimen CC E-2Figure 11. Distribution of  $\varepsilon_{sl}$  over Depth of Cross-Section for  $\lambda = 24$  Specimens

### 3. FE SIMULATION

#### 3.1 Stress-Strain Relationship of Materials

A 5-stage stress-strain relationship of steel material (Han et al. [10]) is used in the FE simulation. The constitutive relationships of the concrete confined by circular CFRP-steel tube under compression as well as under tension (Che et al. [19]) are adopted. The CFRP is assumed to be subjected to tension only, and the stresses in other directions are assumed to be 0.001MPa. Before fracture, the stress-strain relationship is in accordance with Hooke's Law

$$\sigma_{cf} = E_{cf} \varepsilon_{cf} \quad (8)$$

where  $\sigma_{cf}$  and  $\varepsilon_{cf}$  are the stress and the strain of CFRP, respectively. When longitudinal CFRP reaches its rupture strain ( $\varepsilon_{cfr}$ ), it loses longitudinal strengthening effect to the specimens. When transverse CFRP reaches its rupture strain ( $\varepsilon_{cfr}$ ), it loses transverse confinement to the steel tube.

## 3.2 FE Model

### 3.2.1 Element type selection and mesh discretization

The adopted element in the mesh of the steel tube is shell element S4 with full integration. Simpson integration with 9 integrating points in the shell thickness direction is used. For the mesh of the concrete, 3-D brick elements C3D8R with reduced integration is used. Membrane element M3D4 with 4-nodes is used for modelling CFRP. The convergent analysis is carried out by using refined mesh in finite element analysis, details can be found in Ref. (Che et al. [19]).

### 3.2.2 Interface model

Hard contact is used for contact interface between the steel tube and the concrete, i.e., the pressure perpendicular to the contact surfaces ( $p$ ) can be transferred completely between the two surfaces. The tangential force between the steel tube and the concrete is simulated by using Columb model, i.e., shear force can be transferred between two contact surfaces. In the tangential direction of the contact surfaces between the end plate and the concrete, there is no slipping, and hard contact assumption is used in normal direction of the contact surfaces.

Figure 12 shows the comparison of the strains between the steel tube and the CFRP, where,  $\varepsilon_l$  and  $\varepsilon_t$  are the longitudinal strain and the transverse strain respectively, and  $\varepsilon_{cfl}$  and  $\varepsilon_{cft}$  are the strains of the longitudinal CFRP and the transverse CFRP, respectively. As shown in Figure 12,  $\varepsilon_{sl}$  and  $\varepsilon_{cfl}$ , as well as  $\varepsilon_{st}$  and  $\varepsilon_{cft}$ , are approximately same. Additionally, after cutting the CFRP-steel tubes into halves after the tests, it is found that the adherence between the CFRP and the steel tube is still intact except at the region where CFRP ruptured. All above indicate that the steel tubes and the CFRP could cooperate well in both longitudinal and transverse directions. Studies on CF-CFRP-ST stub column (Che et al. [19]; Wang and Shao [34]) and CF-CFRP-ST flexural member (Wang and Shao [28]; Wang et al. [36]) provided same conclusions.

According to the above test results, the CFRP is bound to the steel tube in the finite element model, and it is assumed that no slip exists between the CFRP and the steel tube. Same nodal freedoms are used for the contact elements between the CFRP and the steel tube.

### 3.2.3 Boundary conditions

Boundary conditions (as shown in Figure 13) are simulated as the same situations in the experimental process. According to the symmetry of both the geometry and the boundary condition, 1/4 of the entire model is selected for FE analysis. On the symmetrical plane of the model, symmetrical constraints are applied. At one end, the displacements in  $x$ -,  $y$ - and  $z$ - directions are all restrained. At the other end, line loading is applied (considering initial eccentricity of  $L/1000$ ). Increment iteration method is used to solve the problem in which controlled displacement loading method is used.

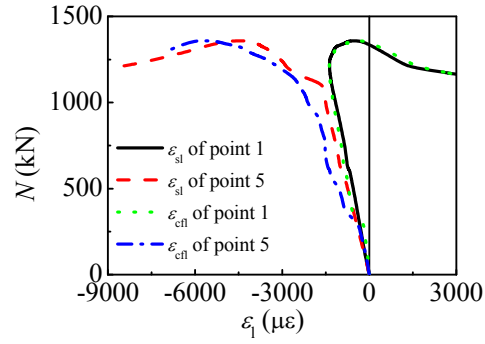
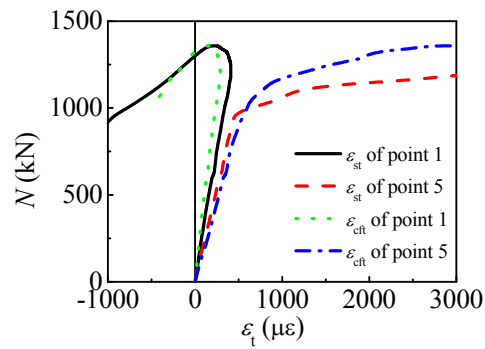
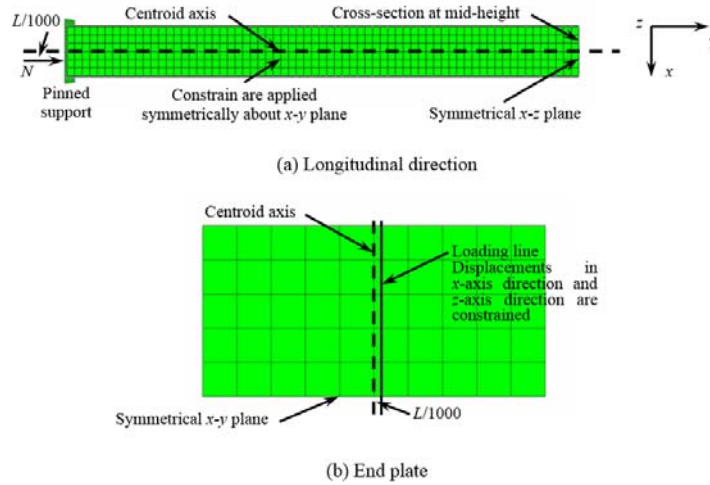
(a)  $N$ - $\varepsilon_l$  Curves(b)  $N$ - $\varepsilon_t$  CurvesFigure 12. Comparisons between  $\varepsilon_s$  and  $\varepsilon_{cf}$  for Specimen CC F-2

Figure 13. Boundary Conditions

### 3.3 FE Results

#### 3.3.1 Failure modes

To verify the reliability of the above presented FE method, overall 32 axially compressed C-CF-CFRP-ST columns are analyzed by using ABAQUS software. Figure 14 shows the deformation modes of the specimen in the test and in FE simulation. From Figure 14, it can be



found that the simulated results agree reasonably well with the experimental results.

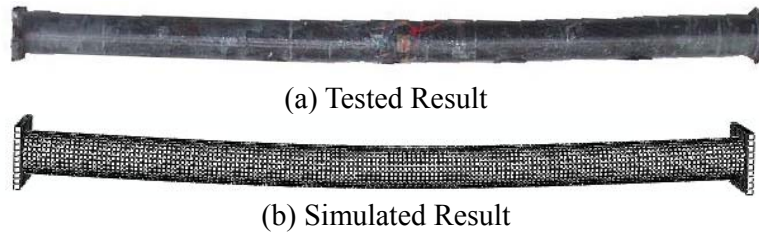
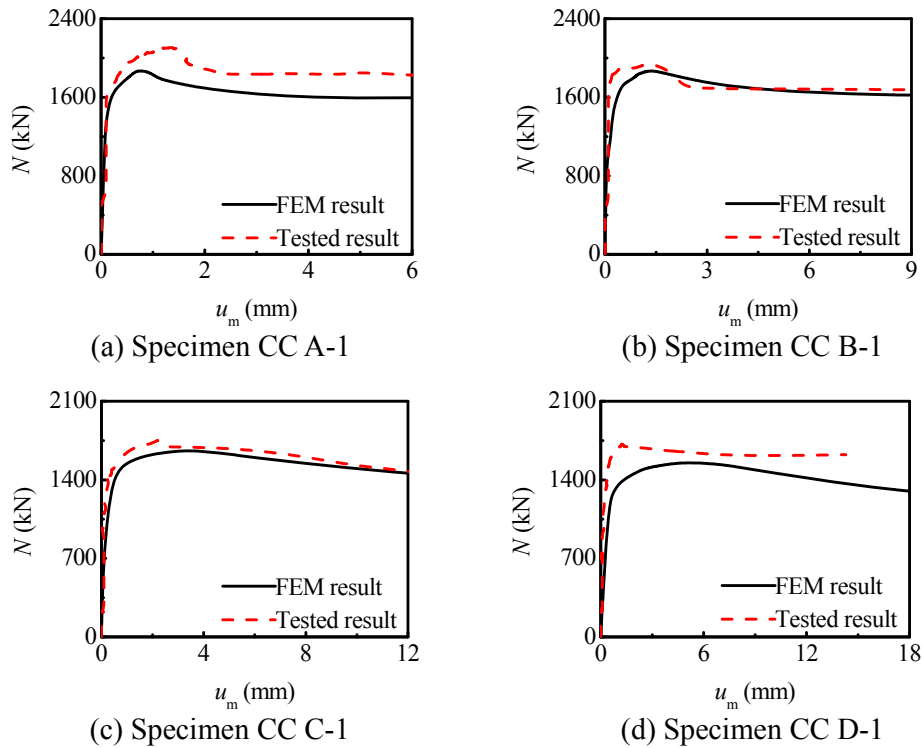
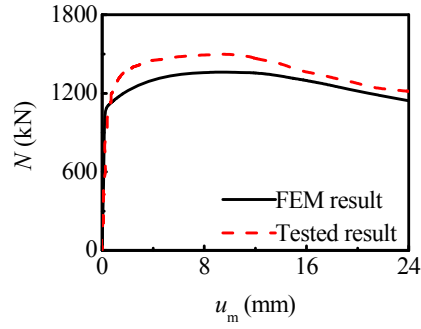


Figure 14. Deformation Modes

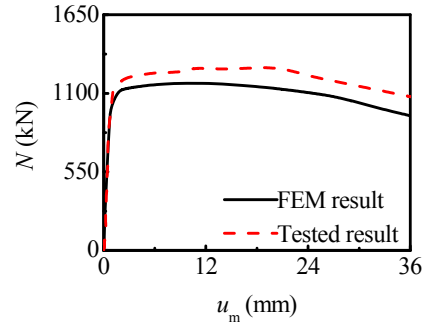
### 3.3.2 $N-u_m$ curves

The FE  $N-u_m$  curves together with the measured results of several specimens are plotted in Figure 15. The FE results agree reasonably well with the experimental results. The average ratio of the critical buckling load between the FE and the experimental results ( $N_{u,cr}^t$ ) is 0.848, and the COV is 0.092. The simulated results for the specimens with large slenderness are relatively smaller, and it is mainly caused by the following reason: The initial eccentricities for all the tested specimen are roughly equal in the experiment. However, such initial eccentricity is prescribed to be  $L/1000$ , which implies that the specimen with a larger slenderness has a bigger initial eccentricity and hence it has a lower simulated result.

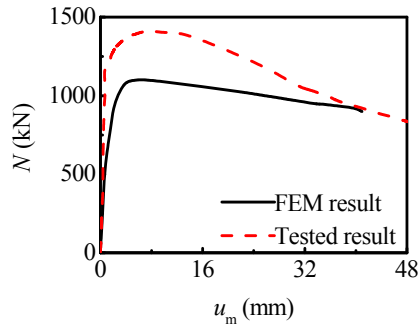




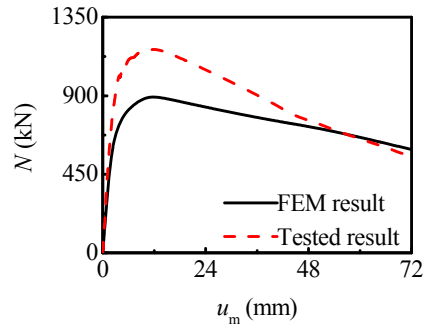
(e) Specimen CC E-1



(f) Specimen CC F-1



(g) Specimen CC G-1

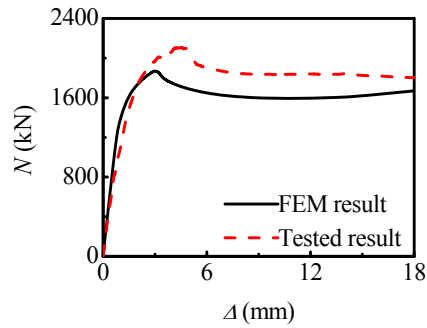


(h) Specimen CC H-1

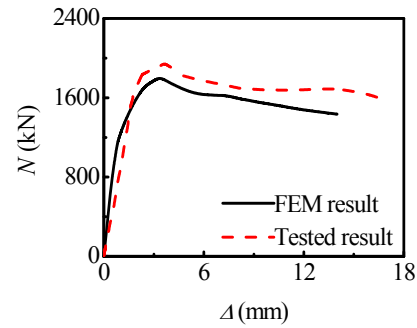
Figure 15. Comparisons of  $N-u_m$  Curves between FEM Result and Tested Result for Several Specimens

### 3.3.3 $N-\Delta$ curves

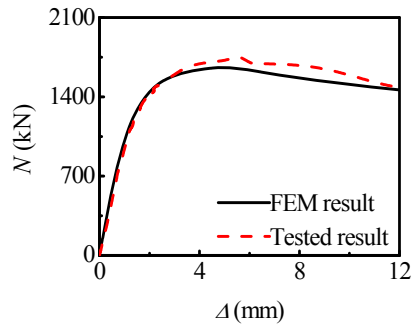
The FE  $N-\Delta$  curves together with the measured results of several specimens are also given in Figure 16. The FE results agree reasonably well with the experimental results.



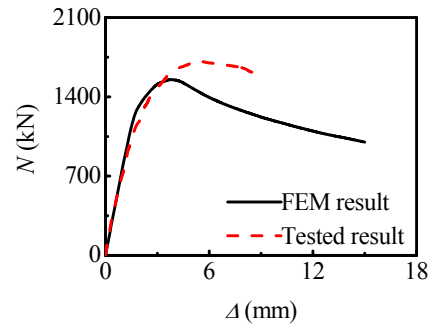
(a) Specimen CC A-1



(b) Specimen CC B-1



(c) Specimen CC C-1



(d) Specimen CC D-1

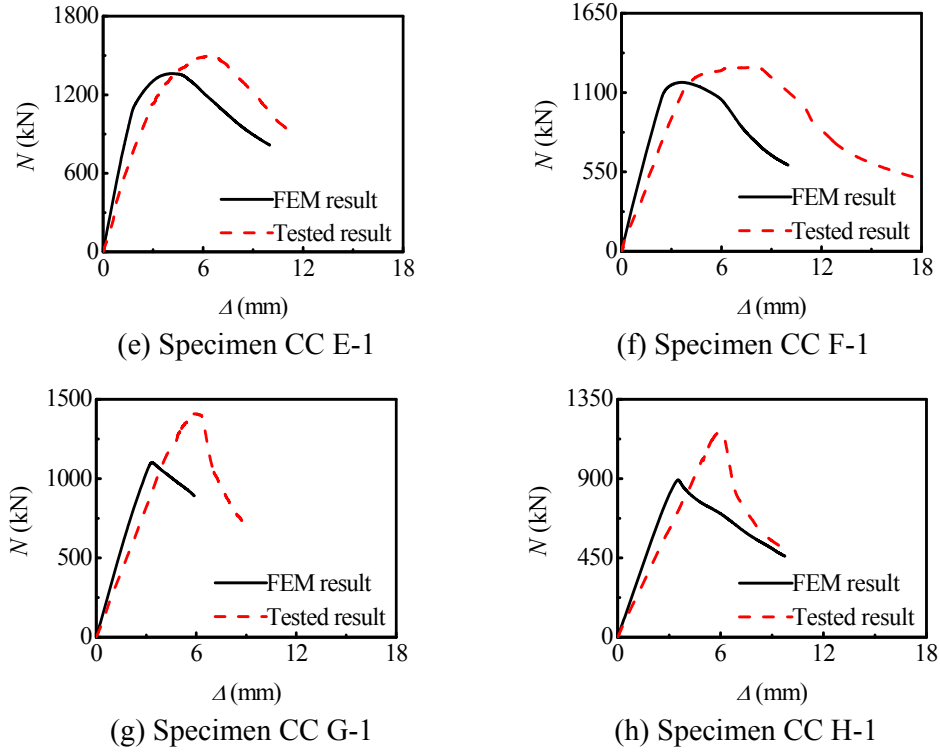


Figure 16. Comparisons of  $N$ - $\Delta$  Curves between FEM Result and Tested Result for Several Specimens

### 3.3.4 $N$ - $\epsilon_s$ curves

The comparison of the strains in the steel tube of specimen CC E-1 is shown in Figure 17. Experimental and FE results are denoted in thin line and in thick line respectively, and the simulated results of the tube strains agree well with the experimental results.

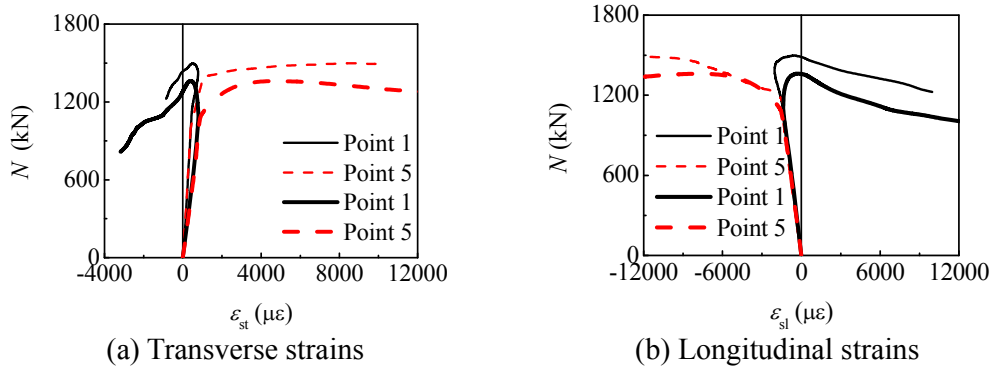


Figure 17. Comparison between Steel Tube Strains of Specimen CC E-1

## 4. THEORETICAL ANALYSIS

On the basis of the above model and approach, a large number of parametric analyses show that the validity range of the models in the presented approach is:  $f_y = 200 - 400 \text{ MPa}$ ,  $f_{cu} = 30 - 120 \text{ MPa}$ ,  $\xi_s = 0.2 - 4$ ,  $\xi_{cf} = 0 - 0.6$ ,  $\eta = 0 - 0.9$ . In the above validity range, a typical model is selected to carry out theoretical analysis, and the details of the typical model are listed as follows:

$D_s = 400\text{mm}$ ,  $t_s = 9.3\text{mm}$ ,  $f_y = 345\text{MPa}$ ,  $f_{cu} = 60\text{MPa}$ ,  $\lambda = 80$ ,  $\xi_{cf} = 0.0383$ ,  $\eta = 0.163$ , elasticity Poisson's ratio of concrete  $\nu_c = 0.2$ ,  $E_c = 4700\sqrt{f'_c}$  (where  $f'_c$  is the compressive strength of cylinder concrete specimens and its unit is in MPa). Five typical points as shown in Figure 18 are selected for further analysis. In Figure 18, the load is proportional to the lateral deflection before point 1, and the stress of the steel tube reaches its proportional limit at point 1. Plastic region occurs on the cross-section at the mid-height between point 1 and point 2, and the critical buckling load is reached at point 2. Area of the plastic region increases gradually after point 2, and the transverse CFRP on the longitudinally compressive region ruptures at point 3. The longitudinal CFRP on the longitudinally tensile region ruptures at point 4. Deflection at the mid-height is very large (about  $L/25$ ) at point 5.

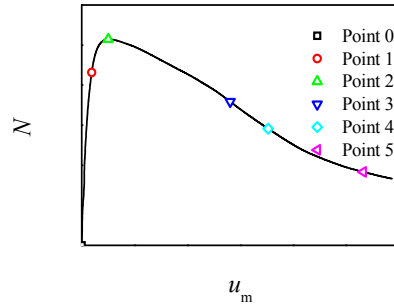


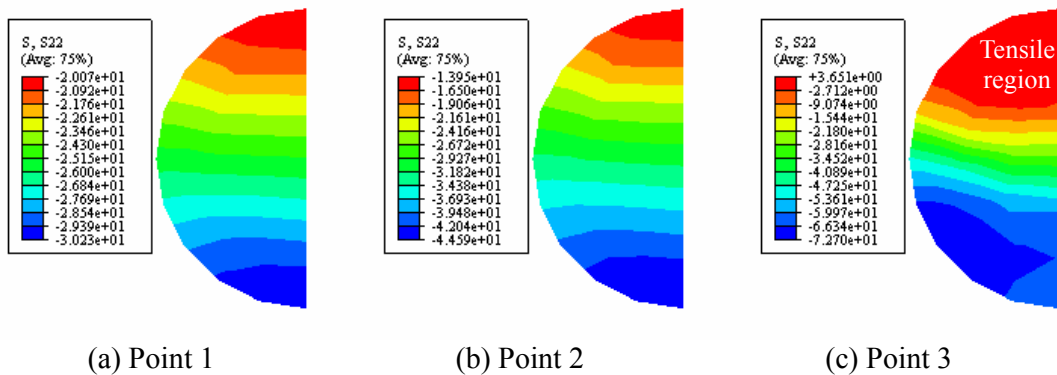
Figure 18. Typical  $N-u_m$  Curve of Axially Compressed C-CF-CFRP-ST Columns with Moderate Slenderness Ratio

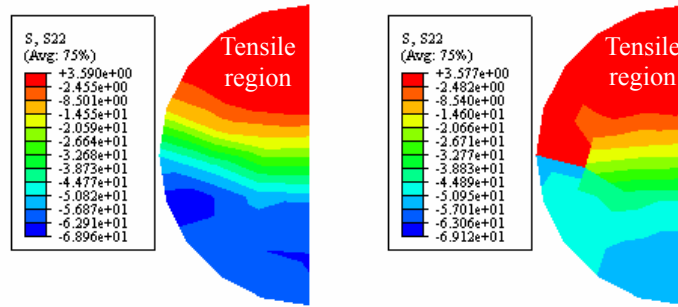
#### 4.1 Stress analysis

##### 4.1.1 Stress in concrete

Figure 19 illustrates the distribution of the longitudinal stress in the concrete on the cross-section at the mid-height for axially compressed C-CF-CFRP-ST column with moderate slenderness ratio. All the cross-section of the concrete is found to be under compression before the critical buckling load is reached. After the critical buckling load, tensile region initiates on the concrete section. With the increasing deflection at the mid-height of the column, the area of the compressive region reduces and the area of the tensile region enlarges continuously.

Figure 20 shows the distribution of the longitudinal stress in the concrete in axial direction. It can be found that such distribution is not uniform and the stresses of the concrete in the compressive region on the cross-section at the mid-height increase gradually.

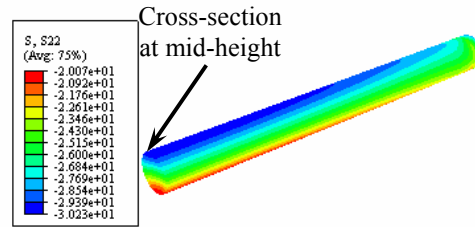




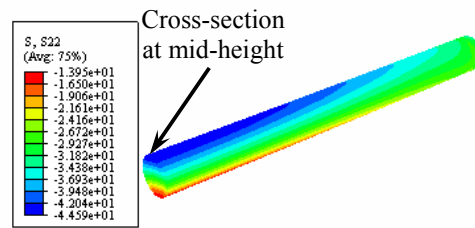
(d) Point 4

(e) Point 5

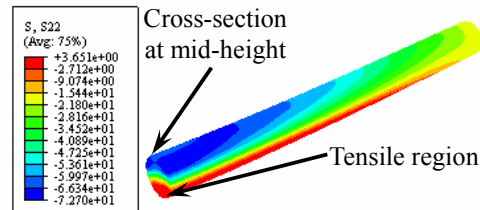
Figure 19. Distribution of Longitudinal Stress in Concrete on Cross-Section at Mid-Height



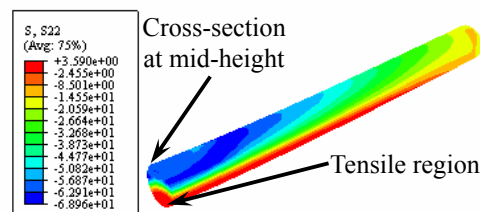
(a) Point 1



(b) Point 2



(c) Point 3



(d) Point 4

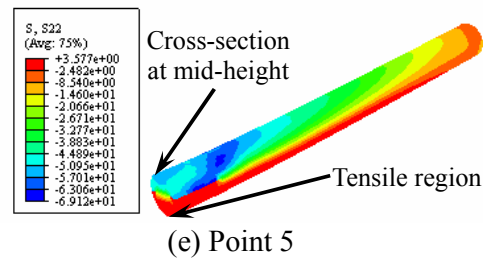
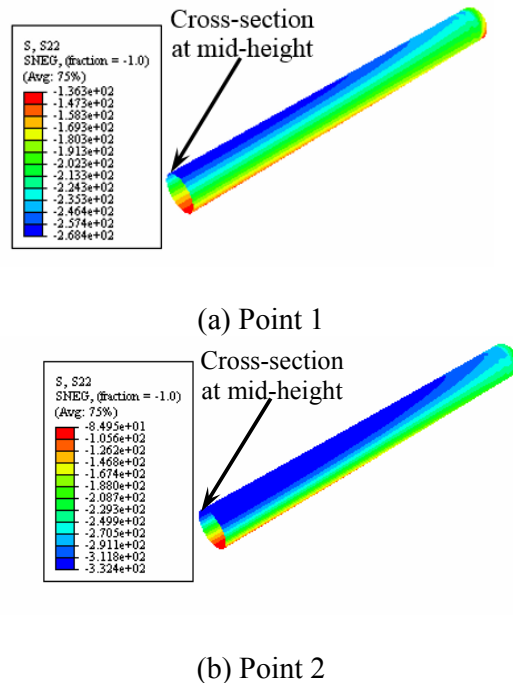


Figure 20. Distribution of Longitudinal Stress in Concrete in Axial Direction

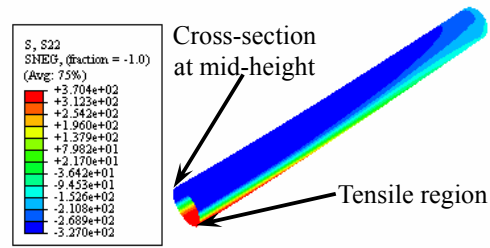
#### 4.1.2 Longitudinal stress in steel tube

Figure 21 shows the distribution of the longitudinal stress in the steel tube in axial direction. The cross-section of the concrete is under compression before the critical buckling load (point 2), while the longitudinal stress on the cross-section varies from compression to tension over the depth on the cross-section after point 3, which process performs from a positive to a negative value of the stresses. The maximum compressive and the maximum tensile stresses are located at the top and at the bottom surfaces respectively.

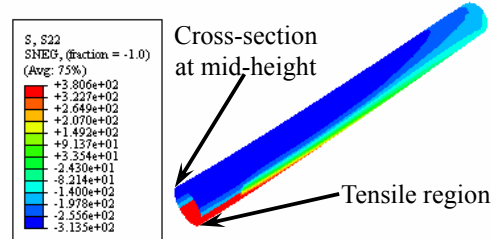
Figure 22 shows the distribution of the Mises stress in the steel tube. The loading at point 1 is relatively smaller and the steel tube is in elastic stage. At point 2, the compressed steel tube begins to yield and the cross-section at the mid-height yields firstly. At this time, the tensioned steel tube does not yet yield. Before the fracture of the transverse CFRP, the compressed steel tube is still in a yielding state. After the fracture of the transverse CFRP, the steel tube enters into a hardening stage.



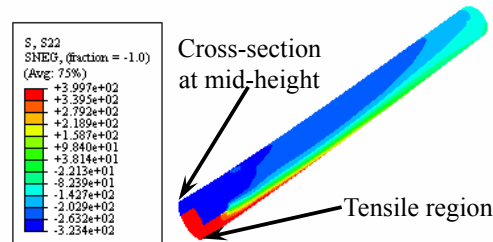




(c) Point 3

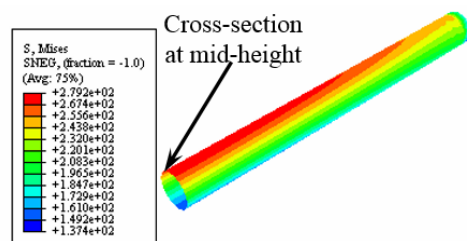


(d) Point 4

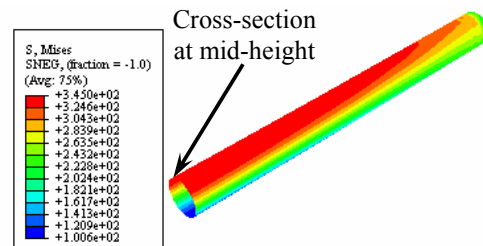


(e) Point 5

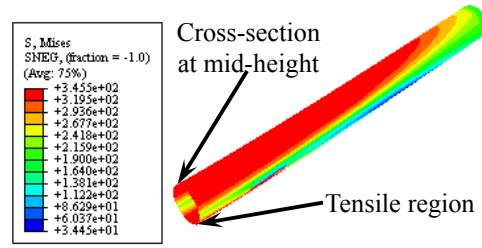
Figure 21. Distribution of Longitudinal Stress in Steel Tube in Axial Direction



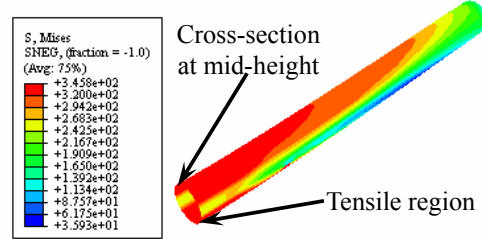
(a) Point 1



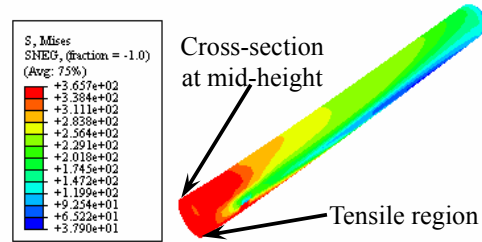
(b) Point 2



(c) Point 3



(d) Point 4



(e) Point 5

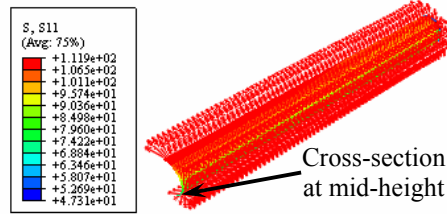
Figure 22. Distribution of Mises Stress in Steel Tube

#### 4.1.3 Stress in CFRPs

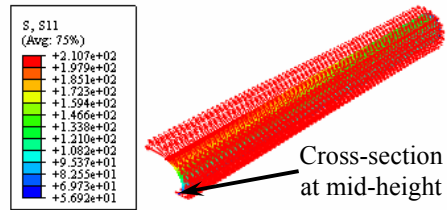
Figure 23 shows the distribution of the stress in the transverse CFRP. Such stress has a uniform distribution in the longitudinal direction in the elastic stage (point 1). Before the critical buckling load, the stress in the compressive region on the cross-section at the mid-height increases gradually. However, the transverse CFRP is still not fractured (the maximum value of stress is about  $0.17 f_{ct}$ ). With the increasing deflection at the mid-height, such stress increases continuously till the CFRP is fractured and does not work (point 3) which indicates that the transverse CFRP in the compressive region in longitudinal direction provides confinement but the transverse CFRP in the tensile region cannot produce such action in the entire loading process.

Figure 24 shows the distribution of the stress in the longitudinal CFRP. It is found that the stress in the longitudinal CFRP has a uniform distribution in the elastic stage (point 1). Before the critical buckling load (point 2), the stress in the tensile region on the cross-section at the mid-height is very small (about 0.001MPa) because the deflection is about only  $L/250$ , which indicates that the longitudinal CFRP does not provide strengthening effect to the column at this time. At point 3, the deflection is about  $L/50$  and the stress in the longitudinal CFRP increases remarkably (the maximum value of the stress is about  $0.57 f_{ct}$ ). With the increasing deflection at the mid-height, the

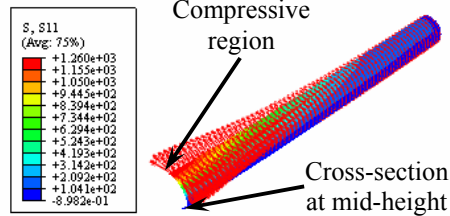
stress in the tensile region increases continuously till the CFRP is fractured and does not work. This shows the longitudinal CFRP in the tensile region detains the flexural deformation of the columns. The longitudinal CFRP in the compressive region cannot produce such action in the entire loading process.



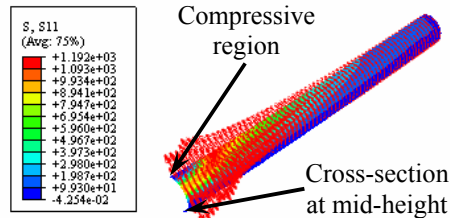
(a) Point 1



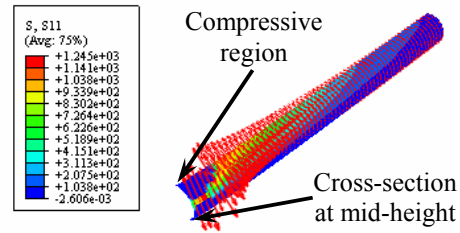
(b) Point 2



(c) Point 3

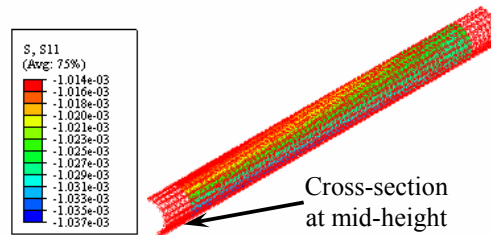


(d) Point 4

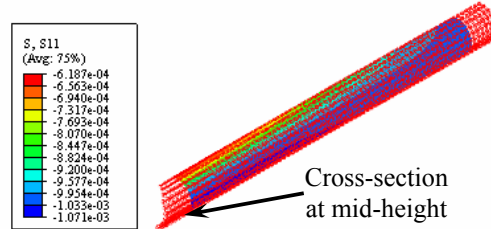


(e) Point 5

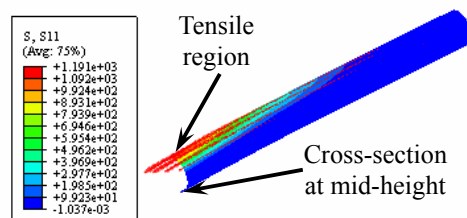
Figure 23. Distribution of Stress in Transverse CFRP



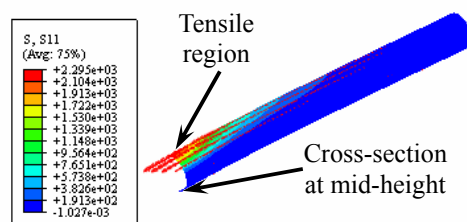
(a) Point 1



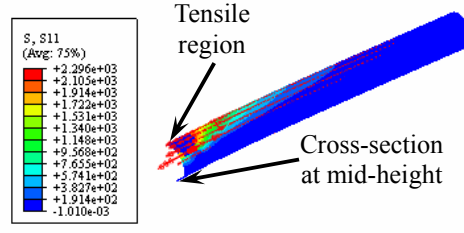
(b) Point 2



(c) Point 3



(d) Point 4



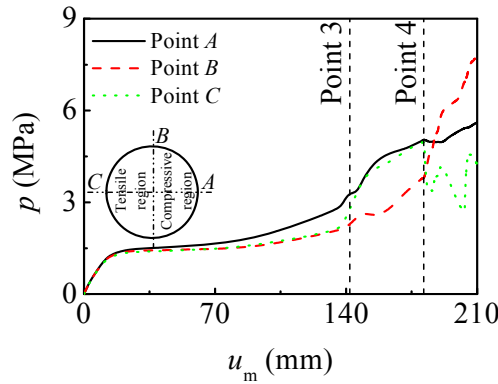
(e) Point 5

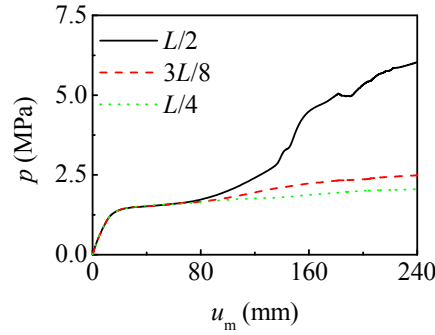
Figure 24. Distribution of Stress in Longitudinal CFRP

#### 4.2 Interaction Force between Concrete and Steel Tube

The interaction force between the steel tube and the concrete ( $p$ )-deflection ( $u_m$ ) curves for points  $A$ ,  $B$  and  $C$  on the cross-section at the mid-height of the column is shown in Figure 25. The interaction force in the compressive region is bigger than the corresponding one in the tensile region before the transverse CFRP in the compressive region (point  $A$ ) is fractured (point 3). After the longitudinal CFRP in the tensile region (point  $C$ ) is fractured (point 4), the interaction force at point  $B$  becomes bigger than the one at point  $A$  because the transverse CFRP at point  $B$  is not fractured and it has still some confinements to the internal C-CFST.

The  $p$ - $u_m$  curves of the columns at a height of  $L/2$ ,  $3L/8$  and  $L/4$  to the end plate respectively in the compressive region are shown in Figure 26. The results show that the interaction force at the mid-height in the compressive region is bigger. With the increasing distance to the mid-height, the interaction force reduces gradually. As seen from Figures 25 and 26, for axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio, the interaction force reduces continuously from the compressive region to the tensile region. In the compressive region, the interaction force also decreases gradually with the increasing distance to the mid-height of the specimens.

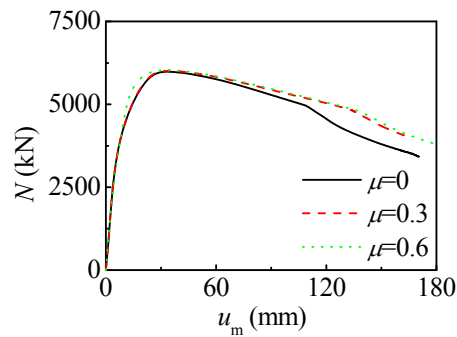
Figure 25.  $p$ - $u_m$  Curves over Depth of Cross-Section of Column

Figure 26.  $p-u_m$  Curves along Height of Column

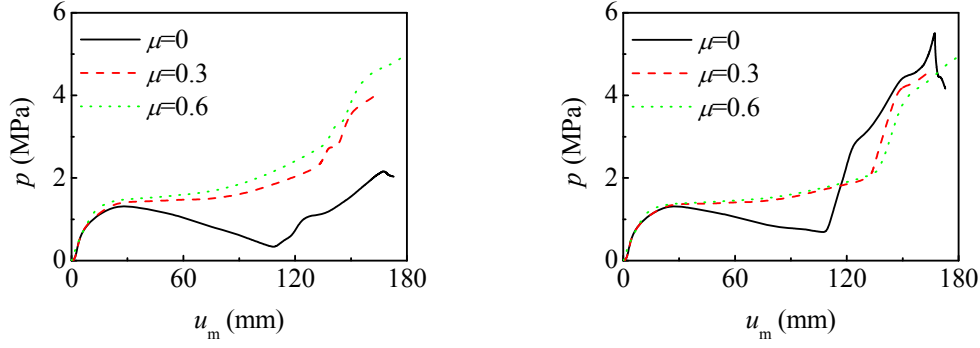
### 4.3 Analysis on Adhesive Strength

To investigate the effect of the adhesive strength between the steel tube and the concrete on the performance of the axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio, different friction factors ( $\mu$ ) with the values of 0, 0.3 and 0.6 respectively are selected in the simulation. Figure 27 shows the effect of the adhesive strength on the  $N-u_m$  curves of the column, which shows that the adhesive strength almost has no effect on the critical buckling load and the stiffness of the specimen in the elastic stage.

Figure 28 shows the effect of the adhesive strength on the  $p-u_m$  curves of the column. In the compressive region,  $p$  increases with the increasing value of the friction factor ( $\mu$ ). A value from 0.3 to 0.6 seems to have no clear effect on  $p$  in the tensile region, which is some different with the case that the value of  $\mu$  is zero.

Figure 27. Influence of Adhesive Strength on  $N-u_m$  Curves of Column





(a) Compressive region (b) Tensile region  
Figure 28. Influence of Adhesive Strength on  $p$ - $u_m$  Curves of Column

## 5. CRITICAL BUCKLING LOAD

### 5.1 Calculation Expression

Many calculated results ( $f_y = 200 - 400 \text{ MPa}$ ,  $f_{cu} = 30 - 120 \text{ MPa}$ ,  $\xi_s = 0.2 - 4$ ,  $\xi_{cf} = 0 - 0.6$ ,  $\eta = 0 - 0.9$ ,  $E_s = 206 \text{ GPa}$ ,  $\nu_s = 0.3$ ,  $\nu_c = 0.2$ ,  $E_c = 4700\sqrt{f'_c}$  MPa) show that the relationship between  $\varphi$  (stability coefficient of the axially compressed C-CF-CFRP-CT columns with moderate slenderness ratio) and  $\lambda$  can be described by using the curve that shown in Figure 29 (a). The curve can be divided into three stages: when  $\lambda \leq \lambda_0$ ,  $\varphi = 1$ , the column fails in strength; when  $\lambda_0 < \lambda \leq \lambda_p$ , the column fails in elasto-plastic buckling; when  $\lambda > \lambda_p$ , the column fails in elastic buckling.  $\lambda_0$  and  $\lambda_p$  are the limited slenderness ratios for an axially compressed C-CF-CFRP-ST column with moderate slenderness ratio in elasto-plastic buckling and elastic buckling respectively, and their values can be determined from the following equations (where the units of  $f_y$  and  $f_{ck}$  are in MPa):

$$\lambda_0 = \pi \sqrt{(420\xi + 550)/f_{cfscy}} \quad (9)$$

$$\lambda_p = 1743 / \sqrt{f_y} \quad (10)$$

where  $\xi$  is the global confinement factor (Che et al. [19]);  $f_{cfscy}$  is the index of load carrying capacity of the axially compressed C-CF-CFRP-ST stub columns (Che et al. [19]), where

$$\xi = \xi_s + \xi_{cf} \quad (11)$$

$$f_{cfscy} = [1.14 + 1.02(\xi_s + 3\xi_{cf})]f_{ck} \quad (12)$$

By using regression analysis method (Han et al. [11]), relationship of  $\varphi$ - $\lambda$  can be expressed as follow

$$\varphi = \begin{cases} 1 & (\lambda \leq \lambda_0) \\ a\lambda^2 + b\lambda + c & (\lambda_0 < \lambda \leq \lambda_p) \\ d/(\lambda + 35)^2 & (\lambda > \lambda_p) \end{cases} \quad (13)$$

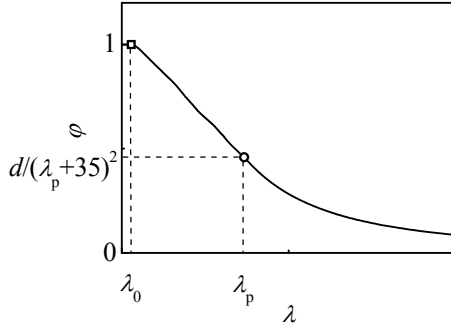
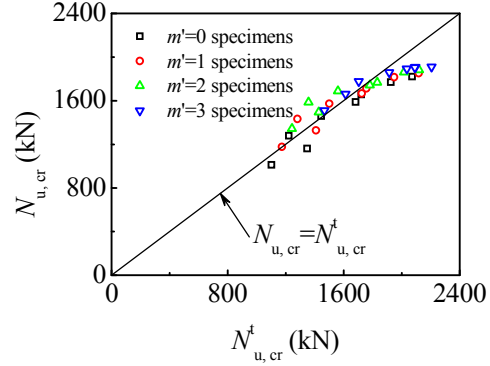
(a)  $\varphi - \lambda$  curve(b) Comparisons between  $N_{u,cr}$  and  $N_{u,cr}^t$ 

Figure 29. Critical Buckling Load

where  $a = [1 + (35 + 2\lambda_p - \lambda_0)e]/(\lambda_p - \lambda_0)^2$ ,  $b = e - 2a\lambda_p$ ,  $c = 1 - a\lambda_0^2 - b\lambda_0$ ,  $e = -d/(\lambda_p + 35)^3$ , the expression of the coefficient  $d$  is obtained from amounts of calculated results based on regression analysis, and it is listed as follow

$$d = \left[ 13000 + 4657 \ln \left( \frac{235}{f_y} \right) \right] \left( \frac{25}{f_{ck} + 5} \right)^{0.3} \left( \frac{\alpha}{0.1} \right)^{0.05} (1 + \eta)^{0.9} \quad (14)$$

where  $\alpha = A_s/A_c$  is the steel ratio.

The expression for the critical buckling load of the C-CF-CFRP-ST columns with moderate slenderness ratio ( $N_{u,cr}$ ) is then expressed as follow

$$N_{u,cr} = \varphi N_u \quad (15)$$

where  $N_u$  is the load carrying capacity of the C-CF-CFRP-ST stub columns (Che et al. [19]),

$$N_u = A_{cfsc} f_{cfscy} \quad (16)$$

where  $A_{cfsc}$  is the cross-sectional area of the C-CF-CFRP-ST columns with moderate slenderness ratio.

## 5.2 Validation of Expression

Figure 29 (b) displays the comparison between  $N_{u,cr}$  and  $N_{u,cr}^t$  for the tested specimens. The average value of  $N_{u,cr}/N_{u,cr}^t$  is 0.97, and the mean square error is 0.08 which means the two results agree well and the calculated results are conservative in overall.

## 6. CONCLUSIONS

Based on the presented results in this study, the following conclusions can be drawn: (1) for the axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio, the specimens tend to fail in strength when the slenderness ratio is small while the ones with large slenderness ratio tend to fail in buckling. Load-deflection curves at the mid-height of the specimens can be divided into three stages: elastic, elasto-plastic and dropping stages. (2) The steel tube and the CFRP tube could cooperate well both in the transverse and in the longitudinal directions. The distribution of the longitudinal strain of the specimens over the depth on the cross-section approximately meets the plane section assumption. The longitudinal and the transverse strains at same point have opposite signs, and the tensioned steel tube in longitudinal direction has no confinement to the concrete. (3) The finite element simulation results of the deformed mode, the  $N-u_m$  curves and the  $N-\Delta$  curves of the members as well as the stresses in the steel tube agree well with experimental results. The stress distributions of different composed materials have been analyzed, and the computed results have a good agreement with experimental results. (4) In the compressive region, with the increasing distance to the mid-height of the specimens, the interaction forces between the outer tube and the concrete reduces gradually. The adhesive strength has almost no effect on the critical buckling load and on the stiffness in the elastic stage of the specimens, but it can improve the confinement to the concrete. (5) The calculating equation of the critical buckling load of the axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio is given.

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## NOMENCLATURE

$A_c$	: Cross-sectional area of concrete
$A_{cfl}$	: Cross-sectional area of longitudinal CFRP
$A_{cfsc}$	: Cross-sectional area of C-CF-CFRP-ST columns with moderate slenderness ratio
$A_{cft}$	: Cross-sectional area of transverse CFRP
$A_s$	: Cross-sectional area of steel tube
C-CF-CFRP-ST	: Circular concrete filled CFRP-steel tubes
C-CFST	: Circular concrete filled steel tubes
CF-CFRP-ST	: Concrete filled CFRP-steel tubes
CF-FRP-T	: Concrete filled FRP tubes
CFRP	: Carbon fiber reinforced plastic
CFST	: Concrete filled steel tubes
$D_s$	: Outer diameter of steel tube
$E_c$	: Elasticity modulus of concrete
$E_{cf}$	: Elasticity modulus of carbon fiber sheets
$E_s$	: Elasticity modulus of steel tube
$f_{cfl}$	: Ultimate tensile strength of longitudinal CFRP

$f_{cfscy}$	: Index of load carrying capacity of axially compressed C-CF-CFRP-ST stub columns
$f_{cft}$	: Ultimate tensile strength of transverse CFRP
$f_{cf}'$	: Tensile strength of carbon fiber sheet
$f_{ck}$	: Characteristic axial compressive strength of concrete
$f_c'$	: Compressive strength of cylinder concrete specimens
$f_{cu}$	: Cubic strength of concrete specimen
FRP	: Fiber reinforced plastic
$f_y$	: Yield strength of steel tube
GFRP	: Glass fiber reinforced plastic
$L$	: Length of specimens
LVDT	: Linear variable differential transformer
$m$	: Number of transverse CFRP layer
$m'$	: Number of longitudinal CFRP layer (s)
$N$	: Axial load
$N_u$	: Load carrying capacity of C-CF-CFRP-ST stub columns
$N_{u,cr}$	: Calculated value of critical buckling load of C-CF-CFRP-ST columns with moderate slenderness ratio
$N_{u,cr}^t$	: Tested value of critical buckling load of C-CF-CFRP-ST columns with moderate slenderness ratio
$p$	: Interaction force between concrete and outer tube
S-CF-CFRP-ST	: Square concrete filled CFRP-steel tubes
$t_{cf}$	: Thickness of 1 layer carbon fiber sheet
$t_s$	: Wall thickness of steel tube
$u_m$	: Deflection at mid-height of column
$\nu_c$	: Elasticity Poisson's ratio of concrete
$\nu_s$	: Elasticity Poisson' ratio of steel tube
$w_{cf}$	: Density of carbon fiber sheet
$\alpha$	: Steel ratio
$\delta_{cf}$	: Elongation percentage of carbon fiber sheet
$\Delta$	: Axial shortening of specimen
$\epsilon_{cf}$	: Strain of CFRP
$\epsilon_{cfl}$	: Strain of Longitudinal CFRP
$\epsilon_{cflr}$	: Rupture strain of longitudinal CFRP
$\epsilon_{cft}$	: Strain of transverse CFRP
$\epsilon_{cflr}$	: Rupture strain of transverse CFRP
$\epsilon_l$	: Longitudinal strain
$\epsilon_s$	: Strain of steel tube
$\epsilon_{sl}$	: Longitudinal strain of steel tube
$\epsilon_{st}$	: Transverse strain of steel tube
$\epsilon_t$	: Transverse strain
$\phi$	: Stability coefficient of axially compressed C-CF-CFRP-ST columns with moderate slenderness ratio

$\eta$	: Strengthening factor of longitudinal CFRP
$\lambda$	: Slenderness ratio
$\lambda_0$	: Limited slenderness ratio for an axially compressed C-CF-CFRP-ST column with moderate slenderness ratio in elasto-plastic buckling
$\lambda_p$	: Limited slenderness ratio for an axially compressed C-CF-CFRP-ST column with moderate slenderness ratio in elastic buckling
$\mu$	: Friction factor
$\sigma_{cf}$	: Stress of CFRP
$\xi$	: Global confinement factor
$\xi_{cf}$	: Confinement factor of transverse CFRP
$\xi_s$	: Confinement factor of steel tube

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